

# River ecomorphodynamics and bioengineering

(ENV-418, A.Y. 2025-26)

4ETCS, Master option

**Prof. Paolo Perona**

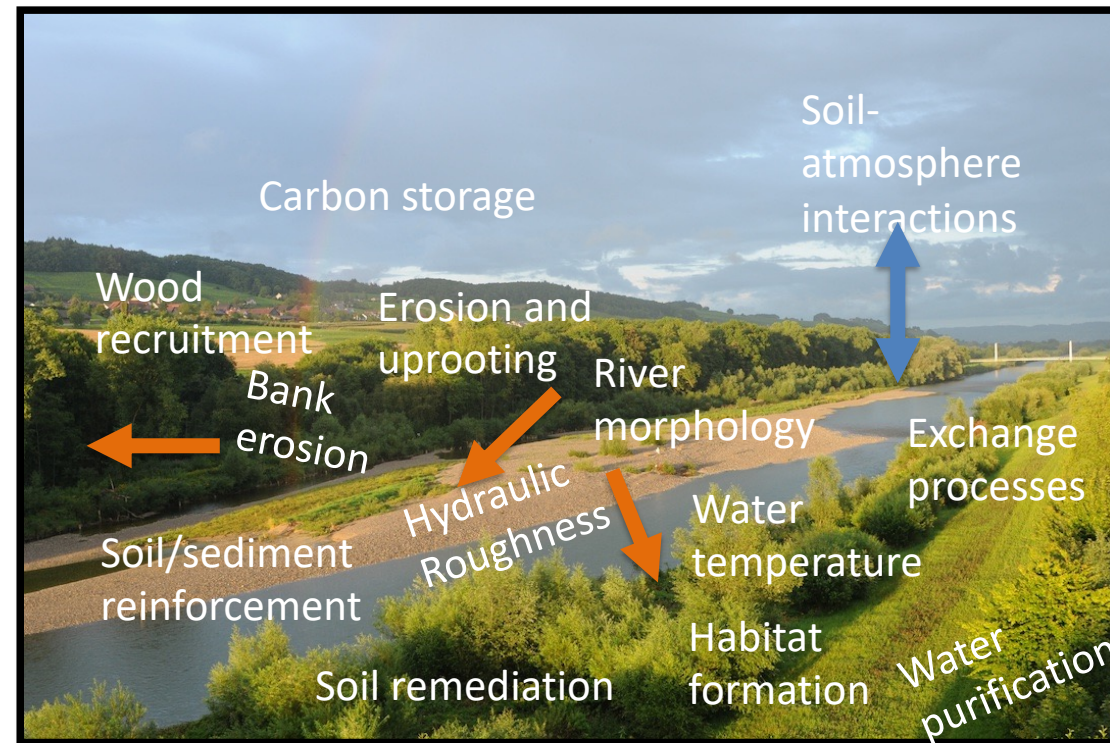
Platform of Hydraulic Constructions



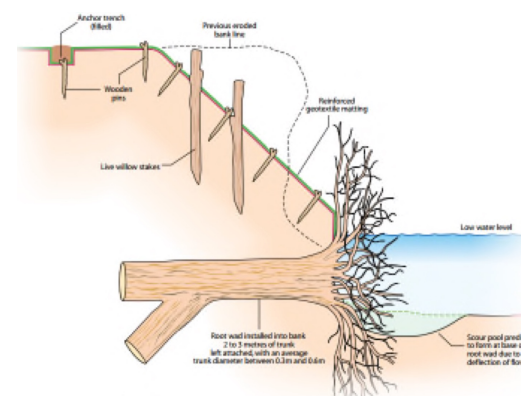
Lecture 12-1: Riparian vegetation,  
canopy and roots

# Interest in riparian vegetation

- Riparian vegetation is an active component with multiple functions for the riverine ecosystems
- Growing next to water courses, it determines both passive and active feedbacks with river dynamics
- Contributes to form river styles and patterns
- Pioneering species contribute to form new habitats (ecological niches)
- Very relevant for sustainable bioengineering approaches but also determines hydraulic risk (bank erosion, LW clogging, etc)



Luther Water, Scotland, UK



# Which riparian plants

- Willows and poplars (Family Salicaceae), several species, fast growth, waterlogging tolerant, etc
- Ubiquitous along river Northern hemisphere, invasive elsewhere
- Pioneer species: keystone succession element
- Ecosystem engineers
- Sprout roots from cutting branches
- Largely used in experimental ecohydraulics

*Populus nigra* (Black populus)



*Salix Alba* (White willow)



Naturally established



Resprout from LW deposits



Bioengineering techniques (cuttings)

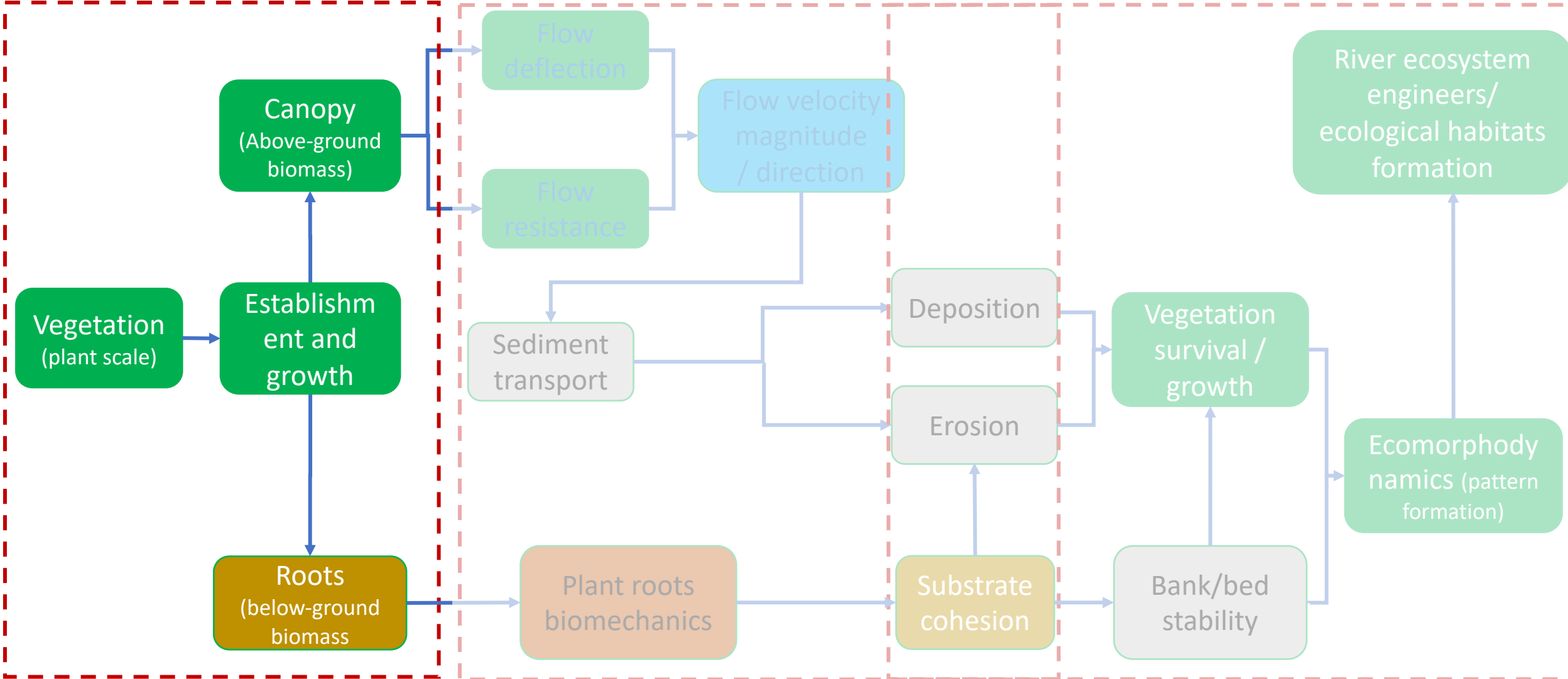


# Salicaceae and fluvial processes

Block lecture 1

Block lecture 2

Block lecture 3

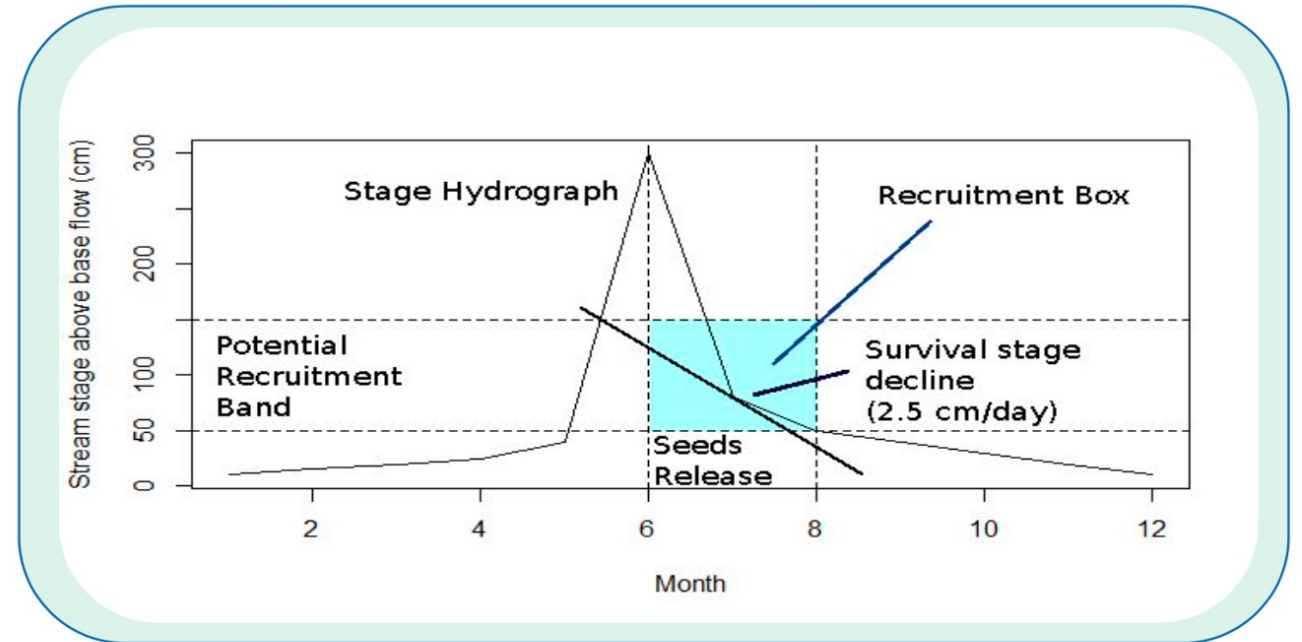


# Above-ground biomass

# Establishment and growth at the field scale

## Seed recruitment

- Salicaceae are heliophilous
  - Require bare ground
- Short-lived seeds ~ 20 days
  - Require moist substrate
- Seeds dispersal sync with annual peak
  - Floods create bare nursery sites
  - Receding wave provides moisture
- Roots track declining stage
  - Max decline 2 - 3 cm/day
  - Max root growth 1.5 - 1.7 cm/day
- Recruitment box model (Mahoney and Rood 1998)
- Recruitment “bands”



Mahoney, J.M., Rood, S.B., 1998. Streamflow Requirements for Cottonwood Seedling Recruitment An Integrative Model. Wetlands 18, 634–645

# Growth of willow cuttings

- 2 Field campaigns (09;10)
- ~ 1200 Salix cuttings in 26 Plots (2m x 2m) with different densities (9 and 20 plants/m<sup>2</sup>)

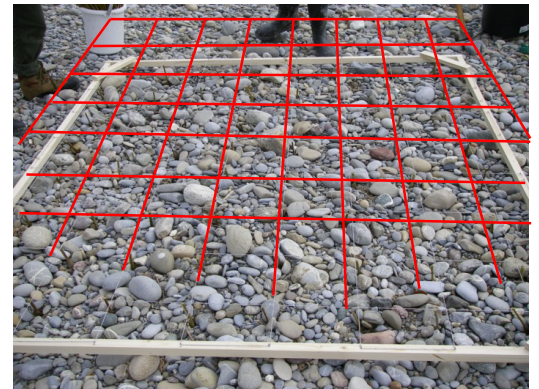
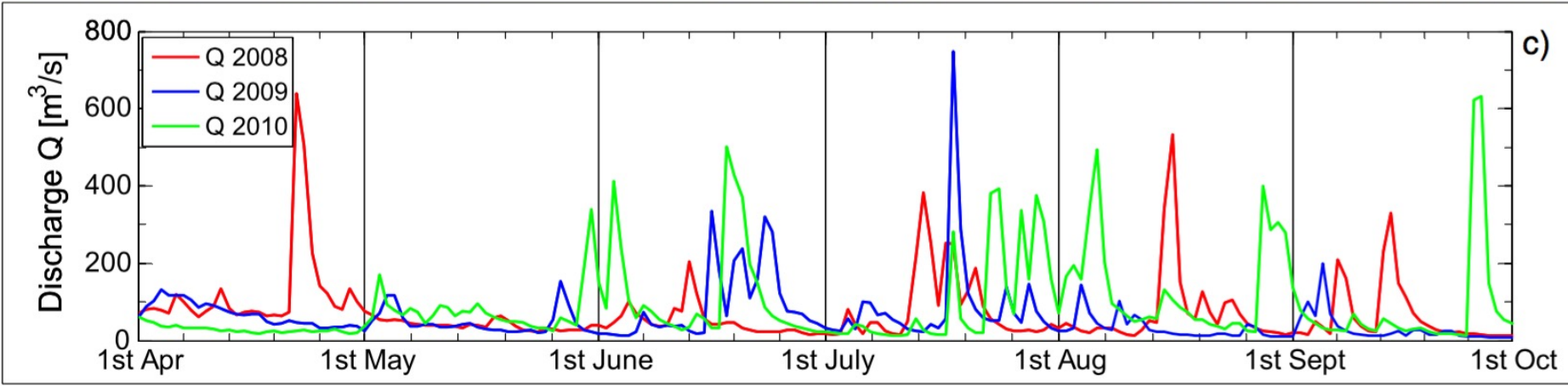
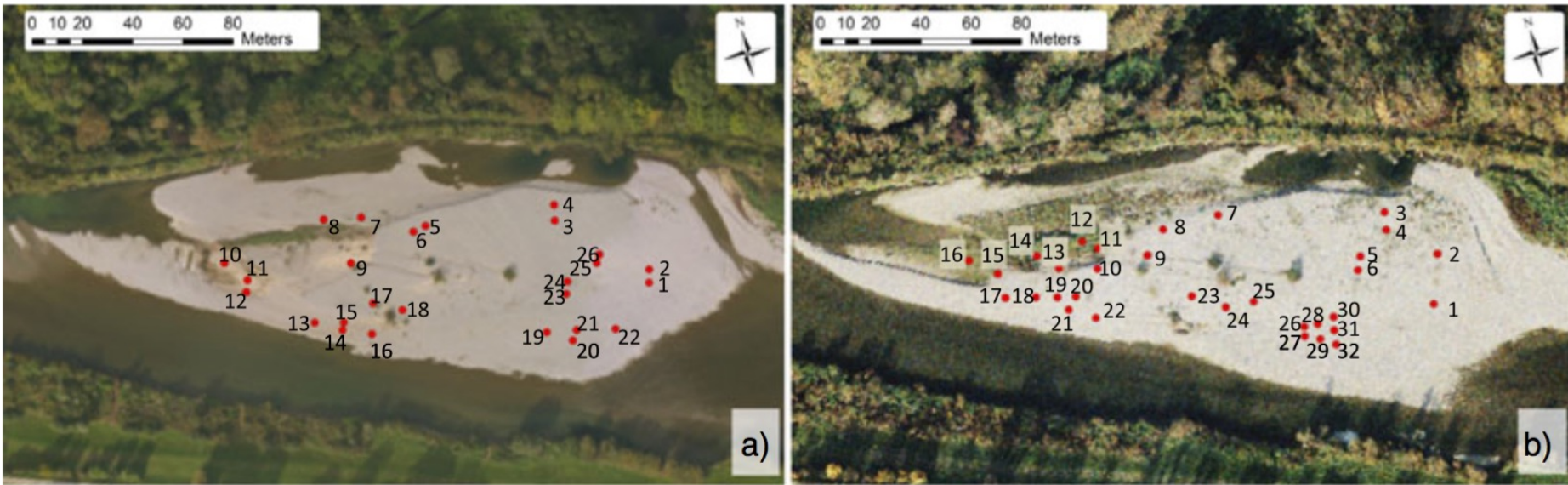
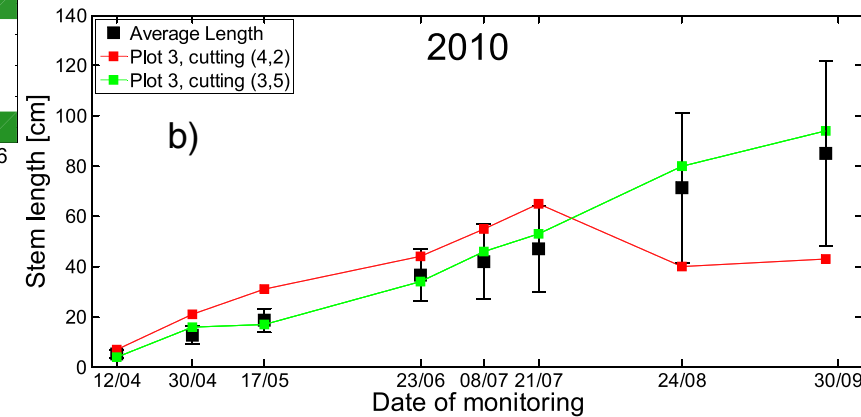
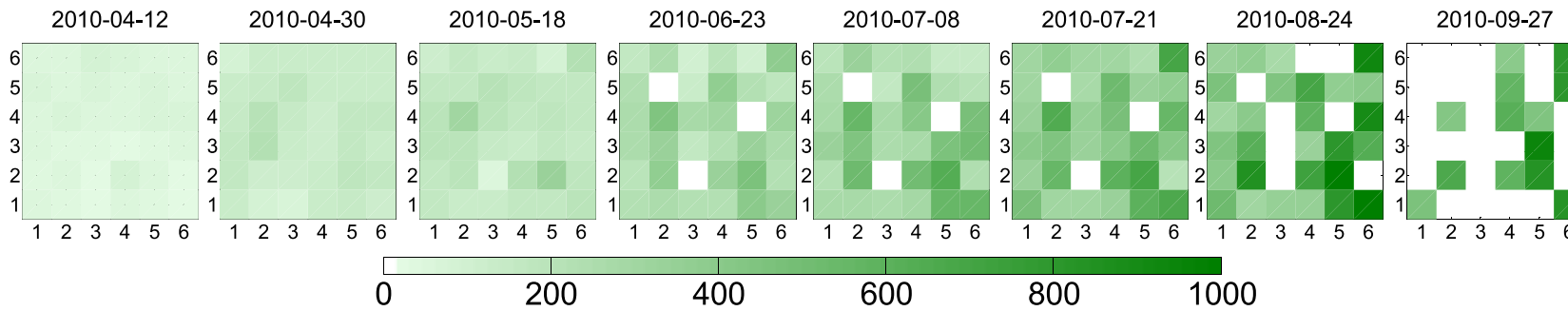
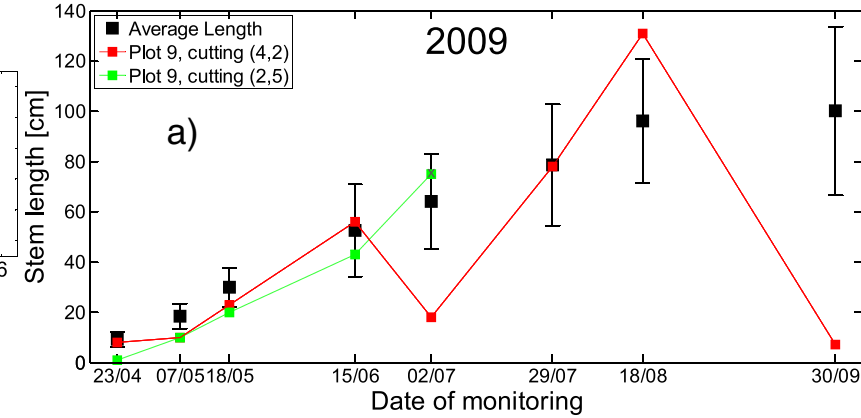
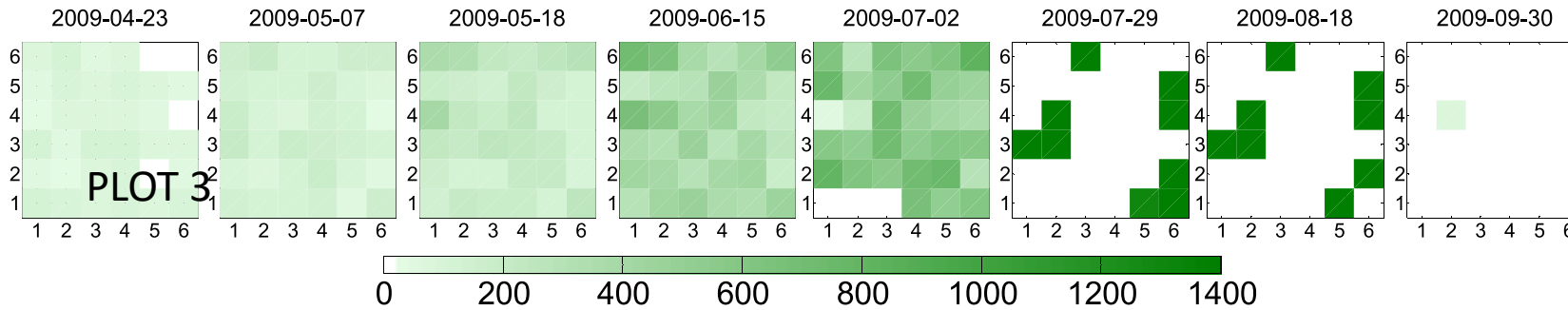


Figure 3. Map of the investigated island showing the location of the vegetation plots in 2009 (a) and 2010 (b). Plot locations have been identified mainly according to hydraulic parameters (flow, shear stress and velocity) and to topography (elevation). Frame (c) shows the hydrographs of the corresponding years

# PLOT 9

From: Pasquale, Perona et al., Hydr. Proc. 2014



Two plots growth dynamics:

Color intensity represents the length of the longest branch in the cutting

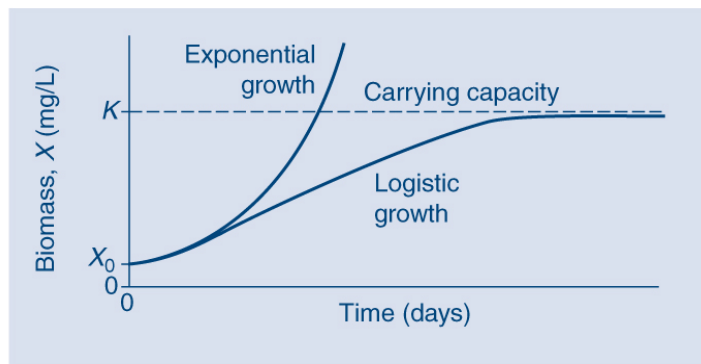
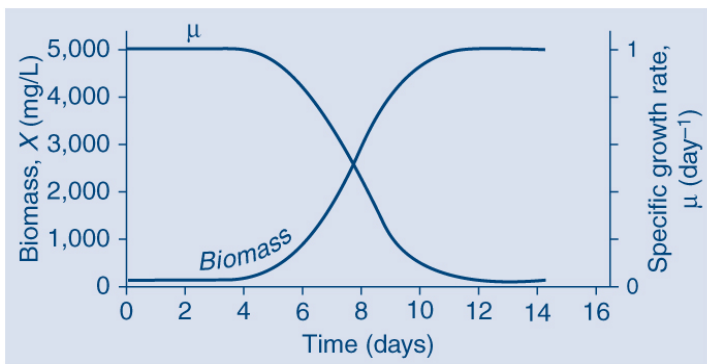
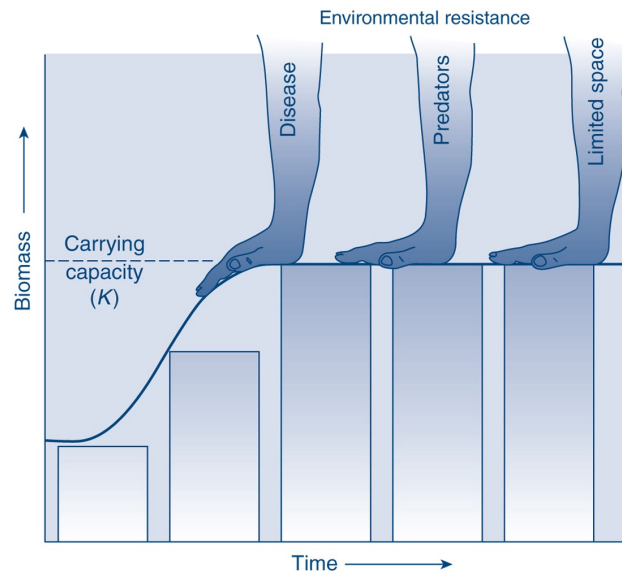
# Logistic growth models

The effect of carrying capacity:  
Logistic growth model

Useful to describe environmental resistance to grow, but no predators

$$\frac{dX}{dt} = (\mu_{\max} - k_d) \left(1 - \frac{X}{K}\right) X$$

$$X(t) = \frac{K}{1 + \left[ \left( \frac{K - X_0}{X_0} \right) e^{-(\mu_{\max} - k_d)t} \right]}$$



## Other similar models

Vegetation growth (Logistic Verhulst equation) and decay (Camporeale, 2006; Perona et al., 2014)

$$\frac{dv}{dt} = v^m (\beta - v)^p \quad \text{Growth}$$

$$\frac{dv}{dt^*} = -\alpha_1 v^n \quad \text{Decay}$$

...or the JABOWA equation (Botkin et al., 1972)

$$\frac{d\vartheta}{dt^*} = \frac{G(\vartheta D_m^*)^{\vartheta-1} \left[ (\vartheta^3 - 2\vartheta^2 + 1)H_m^* - (\vartheta - 1)^2 \vartheta H_0^* \right]}{2 \left[ H_0^* + \vartheta(2\vartheta - 3)(H_0^* - H_m^*) \right] H_m^*}$$

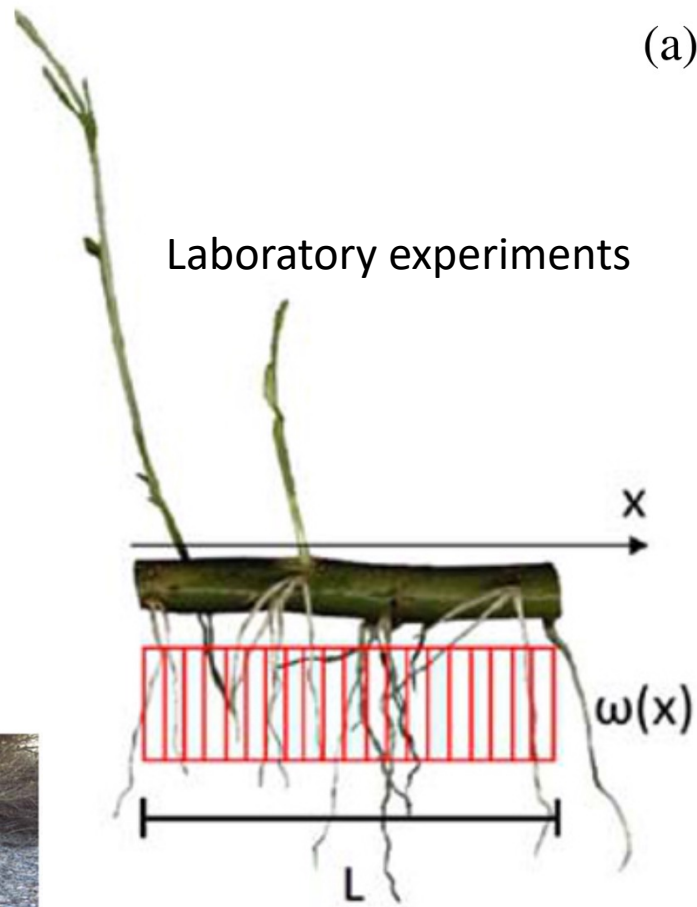
## Discrete logistic map

$$X_{n+1} = a X_n (1 - X_n)$$

Very interesting behaviour for changing a!

# Large wood logs

- LW created & deposited by floods
- ➤ Favourable locations:
  - ○ Low enough to provide moisture
  - ○ High enough to prevent re-mobilization
  - by subsequent floods
- ➤ Key regeneration process in highly dynamic rivers



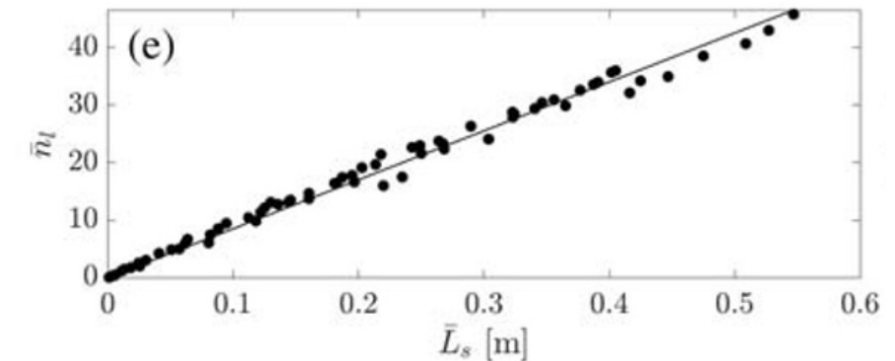
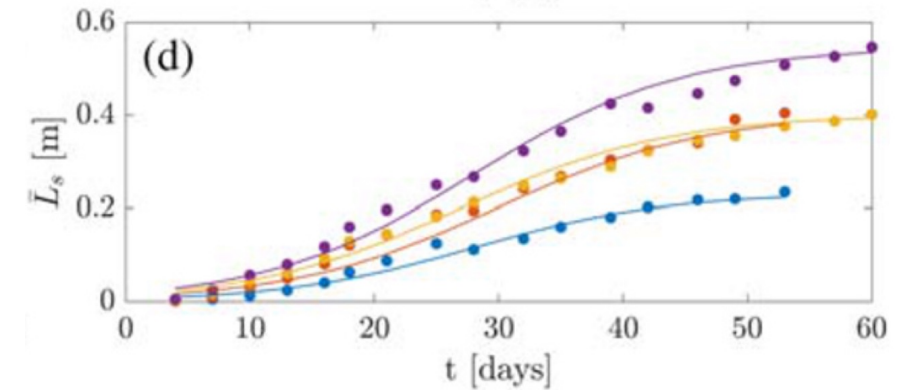
Logistic equation (Verhulst, 1840) for biomass amount  $X(t)$

$$\frac{dX}{dt} = (\mu_{\max} - k_d) \left(1 - \frac{X}{K}\right) X$$

$$X(t) = \frac{K}{1 + \left[ \frac{K - X_0}{X_0} \right] e^{-(\mu_{\max} - k_d)t}}$$

Bau and Perona, JGR 2020

$$\bar{L}_s(t) = \frac{\bar{L}_{s, \max}}{1 + e^{-b(t - t_0)}}$$



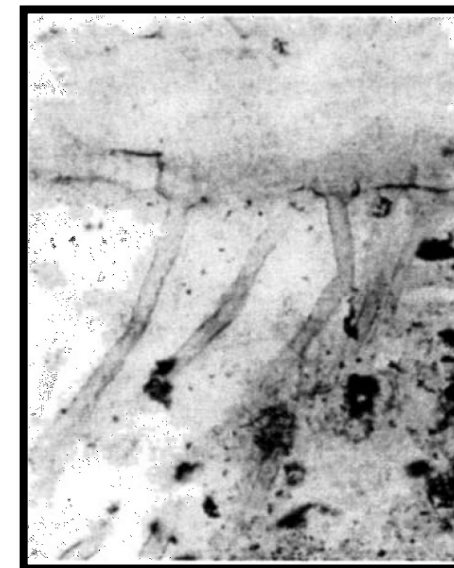
Number of leaves correlates linearly with total stem length

## Below-ground biomass



## Riparian landscapes shaped by plant roots evolution (e.g., Gibling and Davies, Nature Geosci. 2013)

- Definitive early roots in the paleozoic
- Increased biogeomorphic complexity
- Favored aquatic → terrestrial species



## Plant root functions in riparian environments (e.g., Waisel et al.)

- Increase soil cohesion of the riverbank
- Influence biogeochemical processes in the soil
- Sustain below-ground biodiversity



# Paleozoic landscapes shaped by plant roots evolution

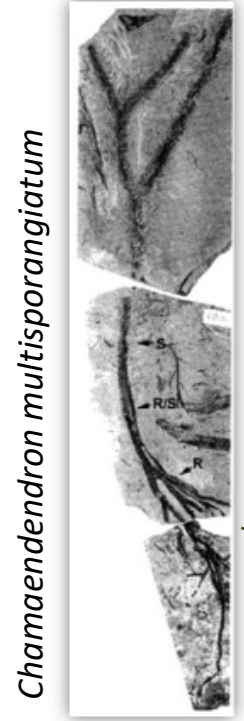
Fluvial style

Plant evolution

Animal evolution



After Davies and Gibling, 2011

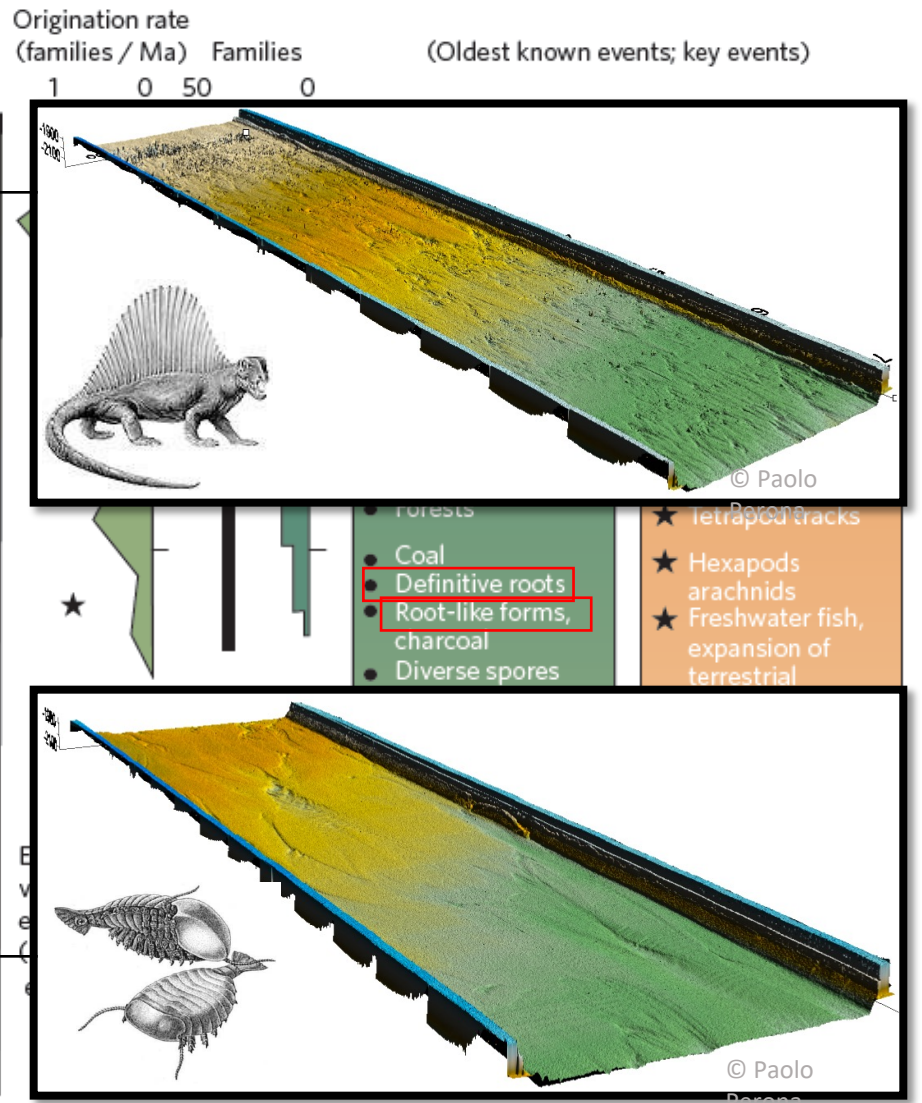
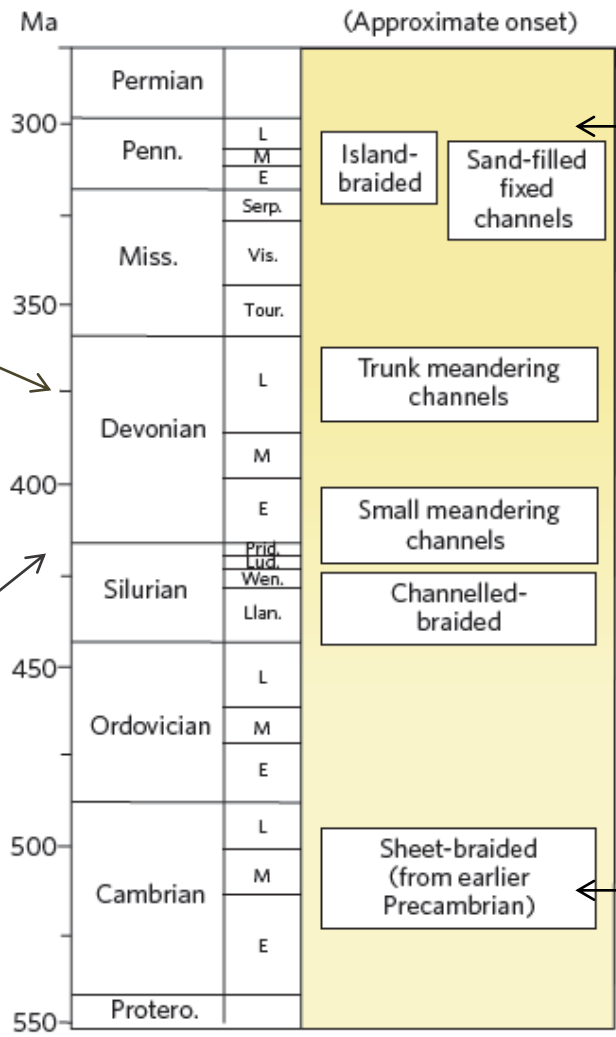


After Gibling and Davies, Nature Geoscience, 2012

From Waisel et al, 2002



Ancient root systems:  
 (Bottom) The oldest (396 Mio ys) rooting structure preserved in growth position; (Top) A 377 Mio-ys-old root of *Chamaendendron multisporangiatum* showing multiple bifurcations on both the root (R) and the Stem (S).  
 Source: [Waisel et al., Plant Roots: the hidden half](#)



# Plant roots growth: tropism actions

“Tropism” is the response of biological systems to environmental stimuli

- Gravitropism (Geotropism): root response to gravity (Knight, 1811)
- Hydrotropism: response to soil moisture gradients (Sachs 1872)
- Phototropism: response to light sources (Darwin, 1881\*)
- Thigmotropism: response to mechanical impedance (Darwin, 1881)
- Oxytropism (aerotropism): response to oxygen concentration (Pfeffer, 1906)
- Chemotropism: response to nutrients (chemicals) concentration
- Plagiotropism: response to temperature gradients (Kaspar and bland 1992)

Pea root growth

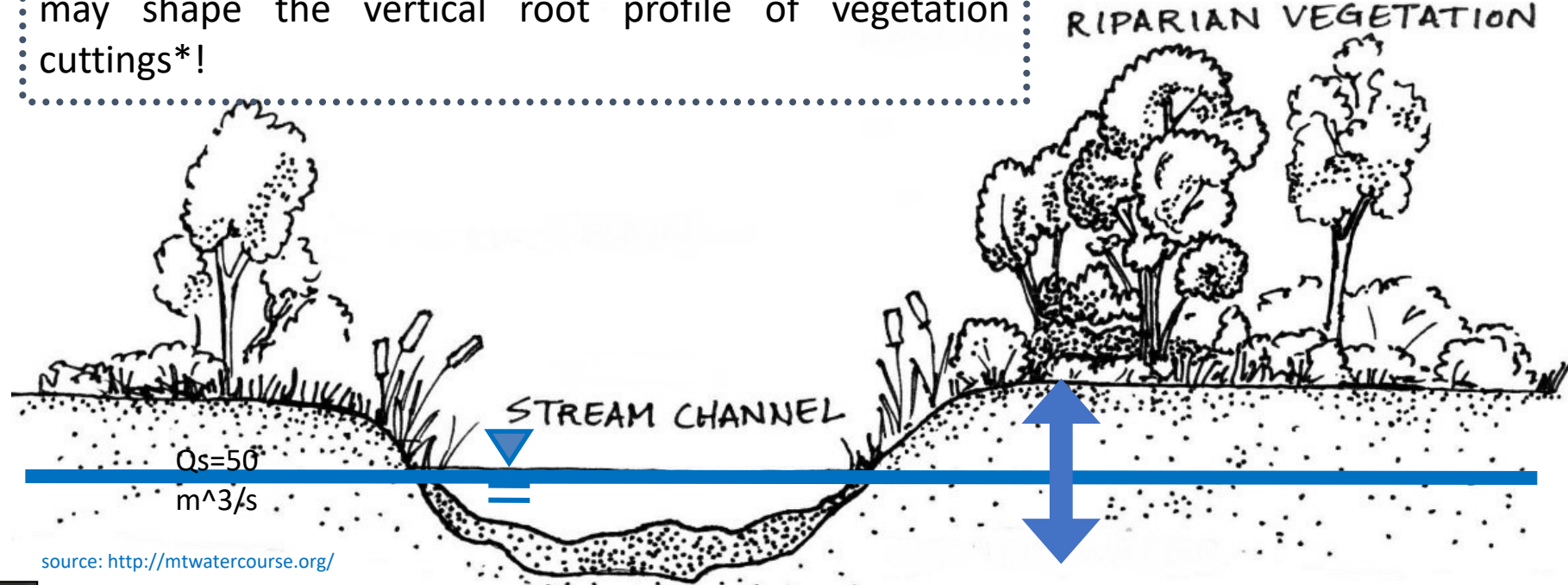
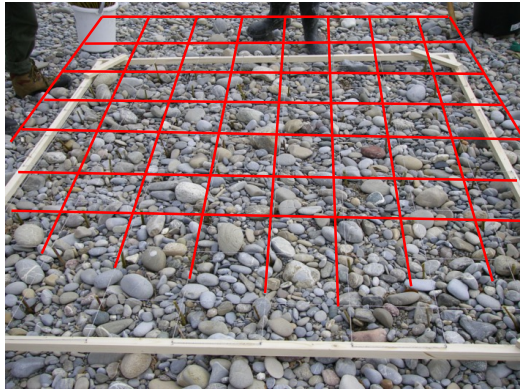


Darwin and Darwin, *The power of movement in plants*, 1881

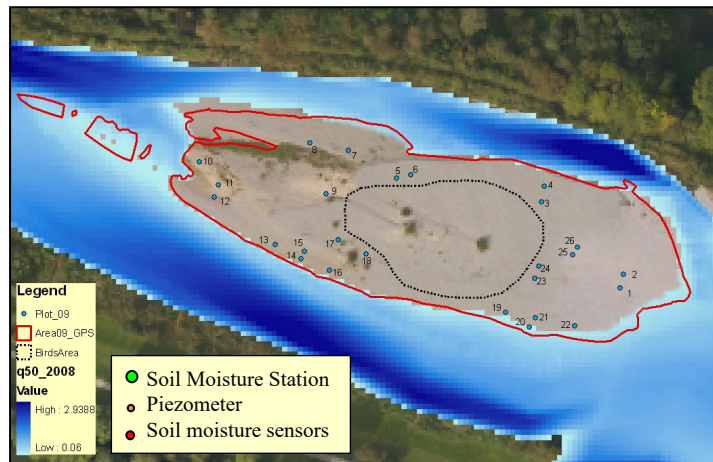
# Root growth



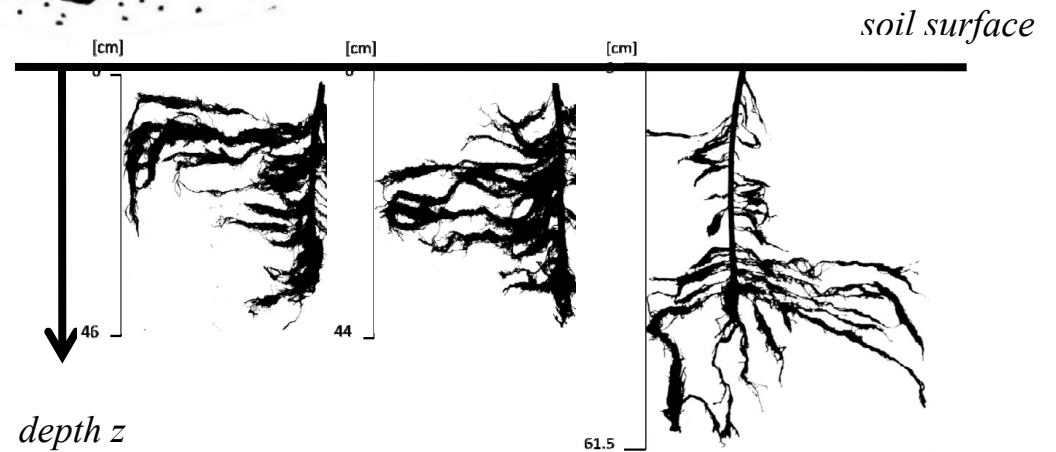
Differently from rainfed upland, river level fluctuations may shape the vertical root profile of vegetation cuttings\*!



source: <http://mtwatercourse.org/>

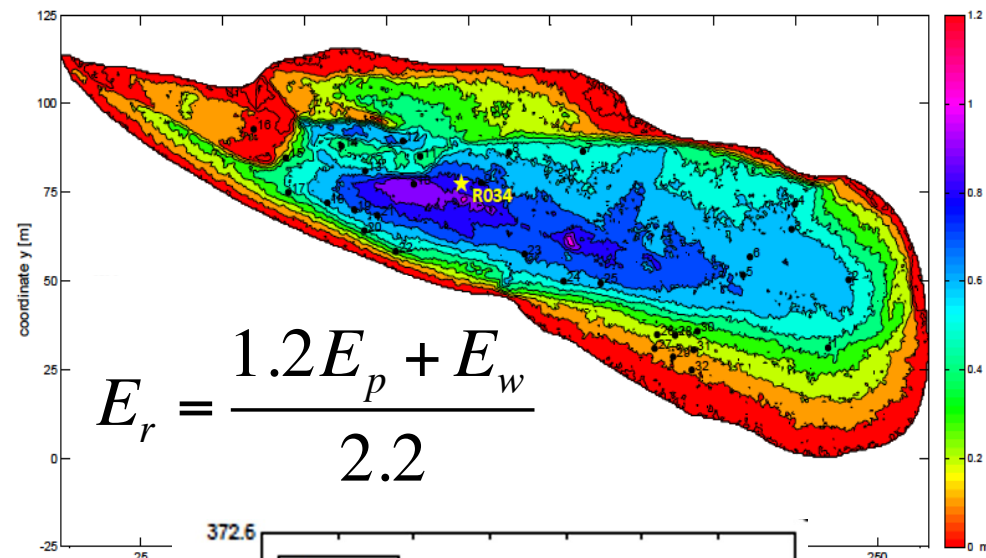
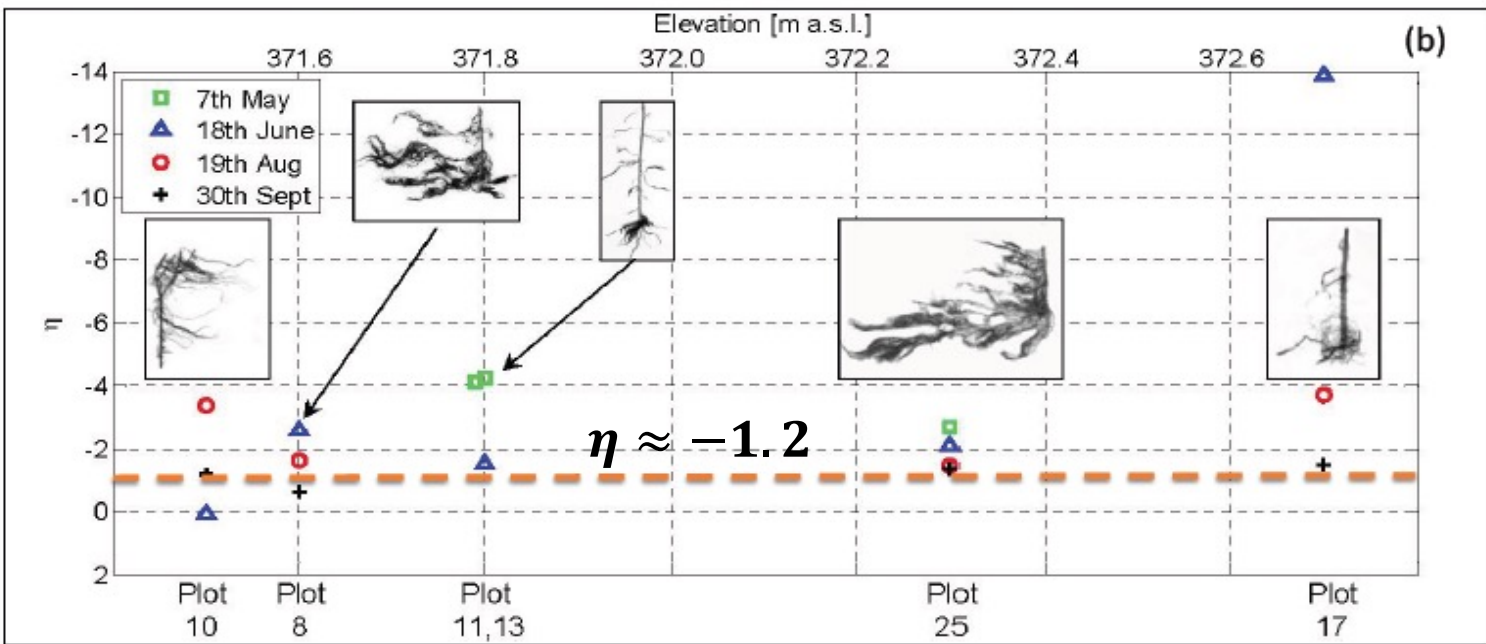
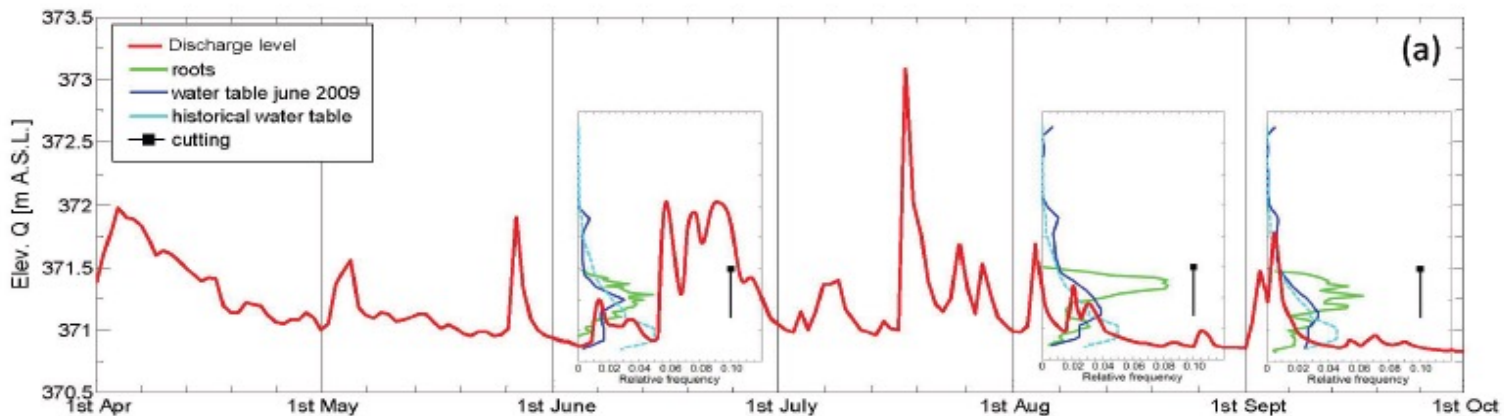


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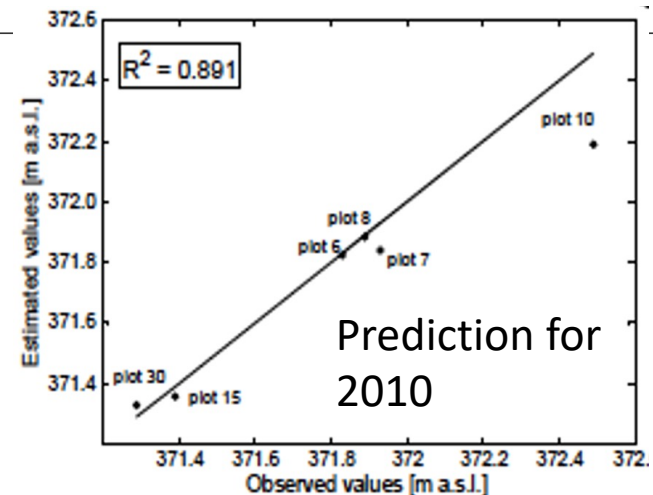


# Dimensionless root mode depth-to-surface

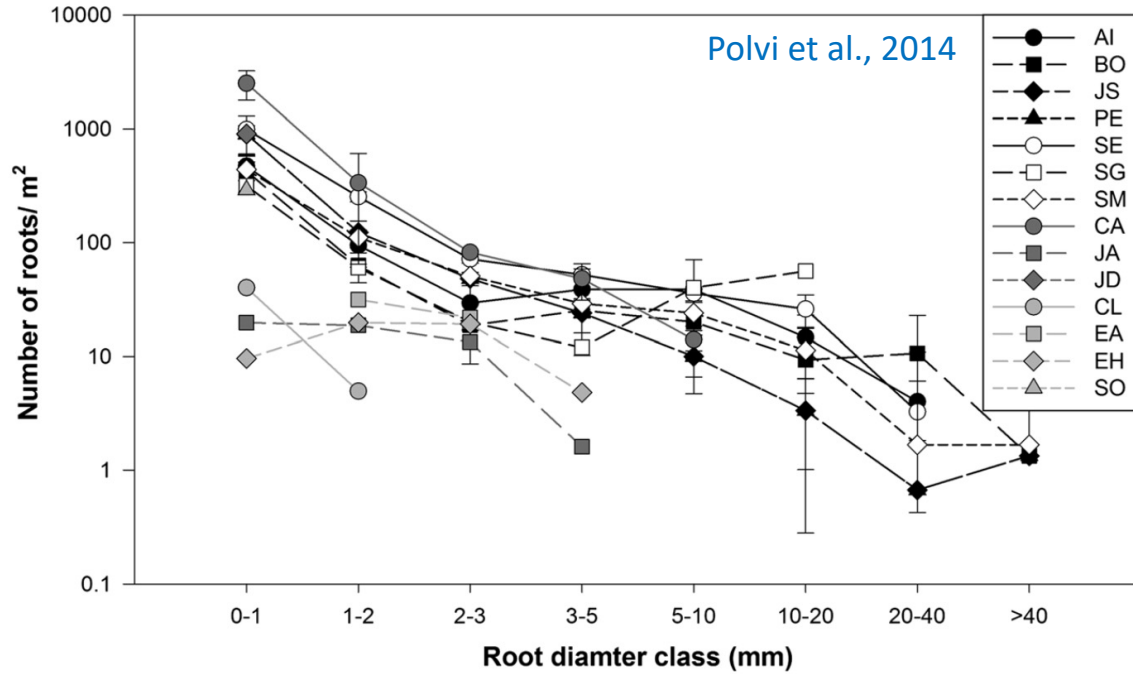
After Pasquale, Perona et al., Ecol. Eng., 2012



$$E_r = \frac{1.2E_p + E_w}{2.2}$$



# Some root characteristics of riparian vegetation

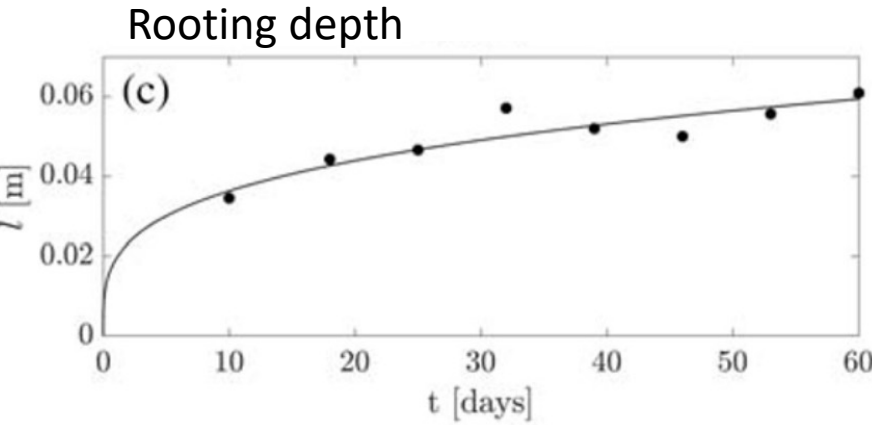
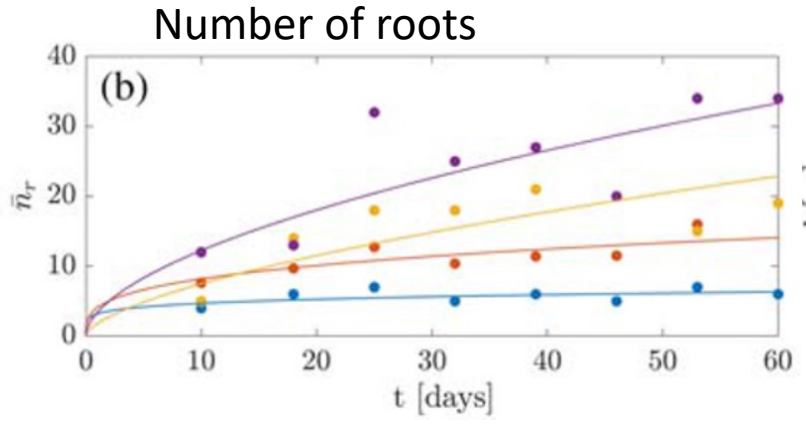
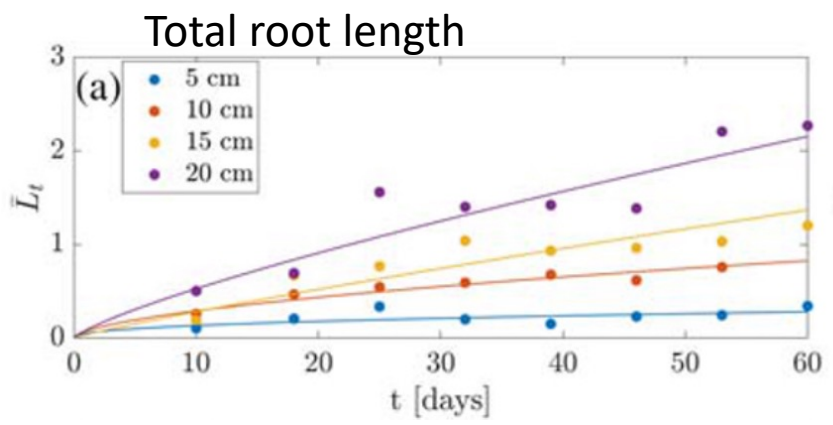
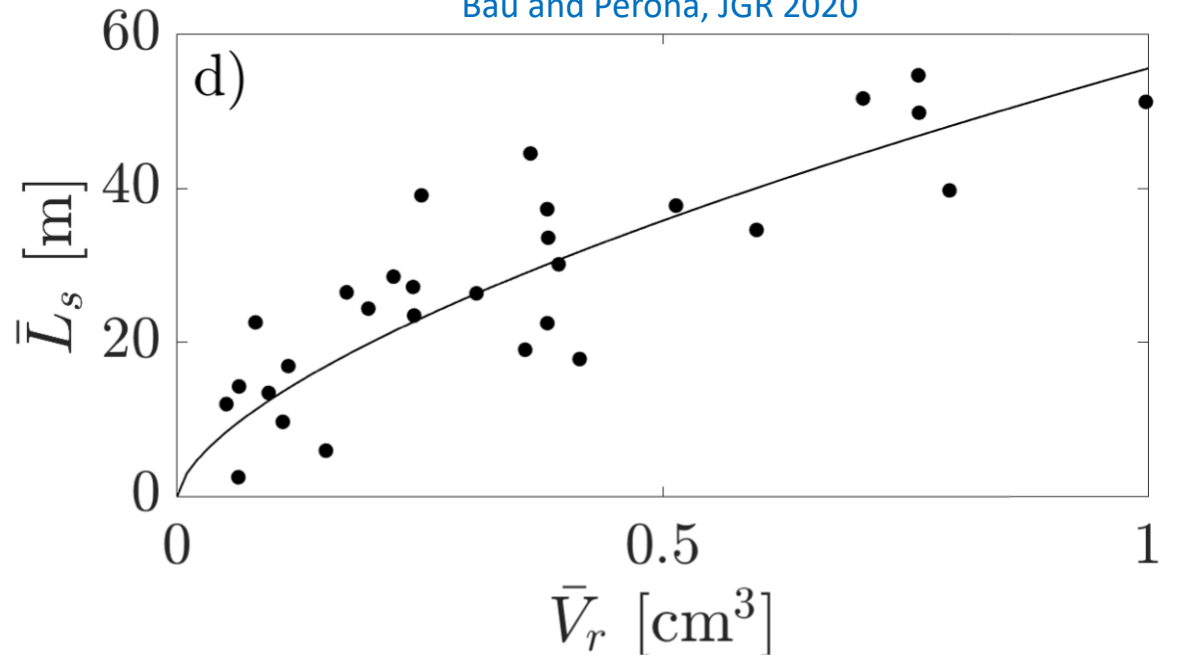
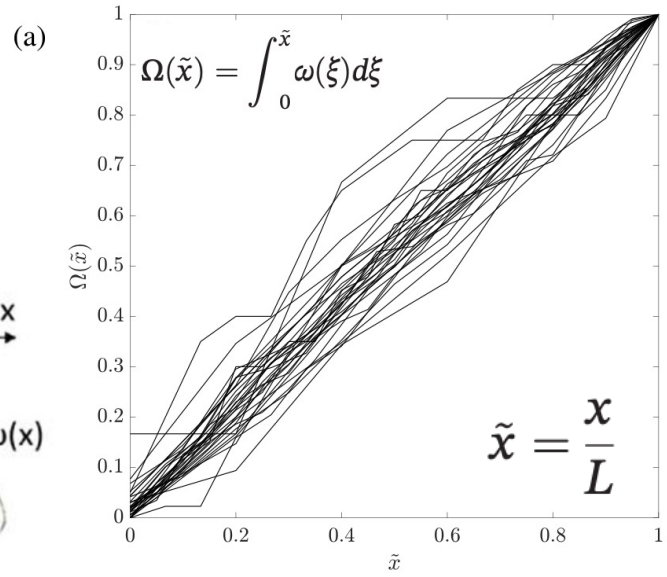
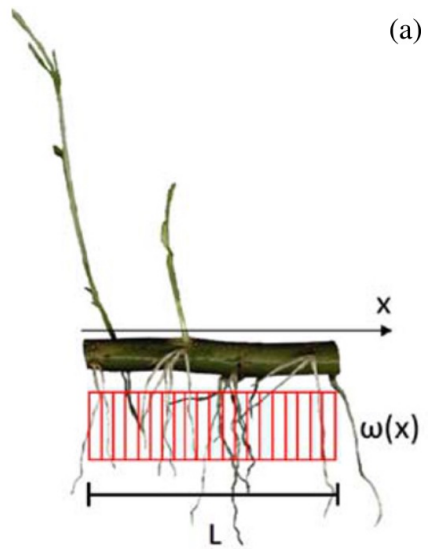


Vegetation group	Root depth (m)				Lateral root extent (m)			
	Min.	Max.	Mean	Range	Min.	Max.	Mean	Range
Tree	0.4	1.0	0.59	0.6	0.5	1.0	0.75	0.5
Shrub	0.2	0.9	0.46	0.8	1.0	1.0	1.00	0.0
Graminoid	0.3	0.6	0.43	0.3	0.1	0.5	0.23	0.4
Forb	0.3	0.5	0.38	0.2	0.1	0.4	0.25	0.3
<i>p</i> -Value			0.181				0.002	

Latin name	Abbreviation	Common name	Vegetation group
<i>Alnus incana</i>	AI	gray alder	Tree
<i>Betula occidentalis</i>	BO	western birch	Tree
<i>Caltha leptosepala</i>	CL	marsh marigold	Forb
<i>Carex aquatilis</i>	CA	water sedge	Graminoid
<i>Equisetum arvense</i>	EA	field horsetail	Forb
<i>Equisetum hyemale</i>	EH	scouringrush horsetail	Forb
<i>Juncus arcticus</i>	JA	arctic rush	Graminoid
<i>Juncus drummondii</i>	JD	Drummond's rush	Graminoid
<i>Juniperus scopulorum</i>	JS	western juniper	Tree
<i>Picea engelmannii</i>	PE	Engelmann spruce	Tree
<i>Salix exigua</i>	SE	sandbar willow	Shrub
<i>Salix geeyeriana</i>	SG	Geyer willow	Shrub
<i>Salix monticola</i>	SM	mountain willow	Shrub
<i>Saxifraga odontoloma</i>	SO	brook saxifrage	Forb

# Re-sprouting of Large Wood Deposits

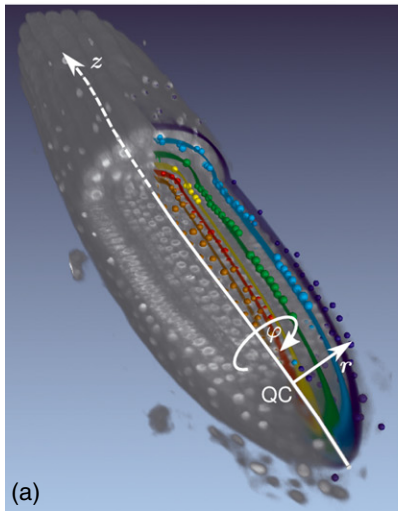
Bau and Perona, JGR 2020



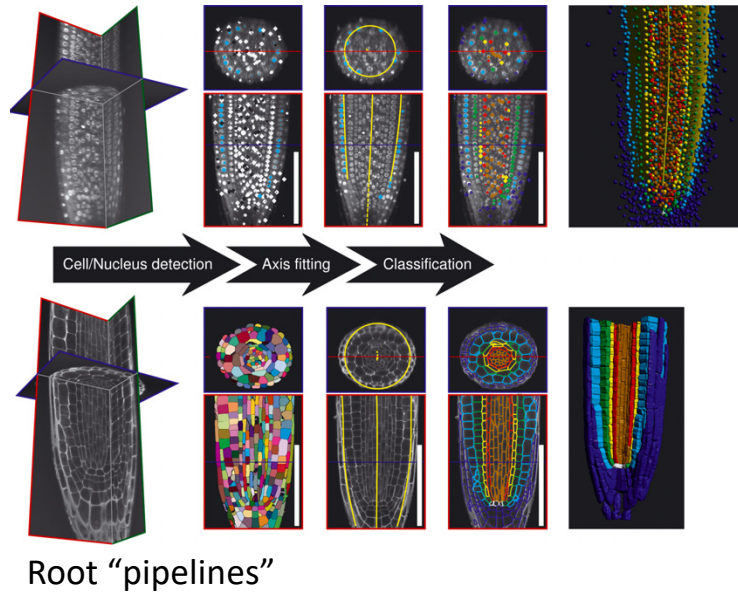
# Root growth models

# Root analysis and architecture models

The iRoCS Toolbox – 3D analysis of the plant root apical meristem at cellular resolution (Schmidt et al., Plant Journal, 2014)

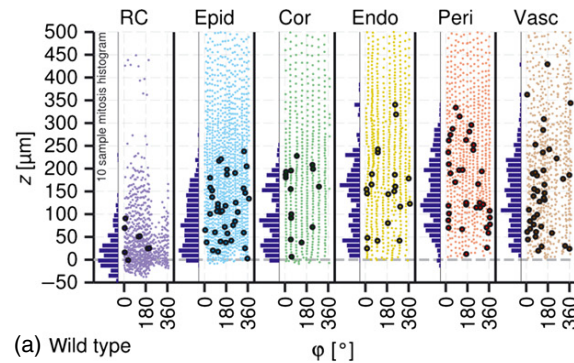


(a) Root description



Root "pipelines"

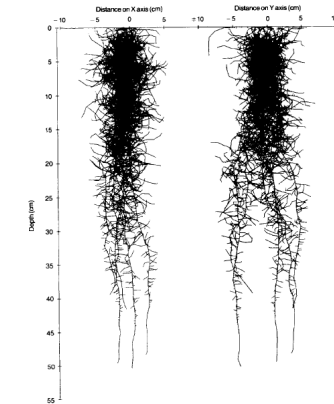
Cumulated median statistics concerning hormon fluxes within cell tissues



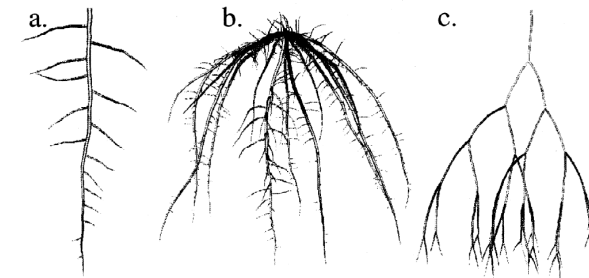
(a) Wild type

- 3D-Geometric models
- Based on a number of predefined (probabilistic) geometric rules, e.g.:
  - Number of branches
  - Branching length
  - Branching angles

**ROOTMAP**  
(The Australian School, Diggle, Plant & Soil, 1988)



**SIMROOT**  
(The American School, Lynch et al., Plant & Soil, 1997)

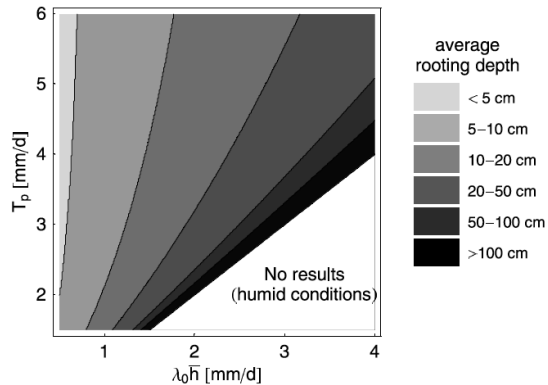
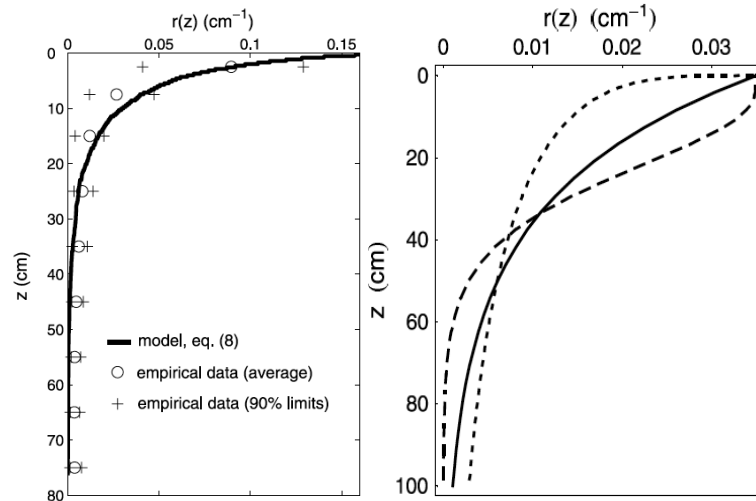


Includes some kinematics functions and generates "solid" 3-D roots

# Root density models (1D)

The Italian School, Ecohydrology  
(Laio, WRR, 2006,  
Laio et al., GRL, 2006; Tron et al., 2014)

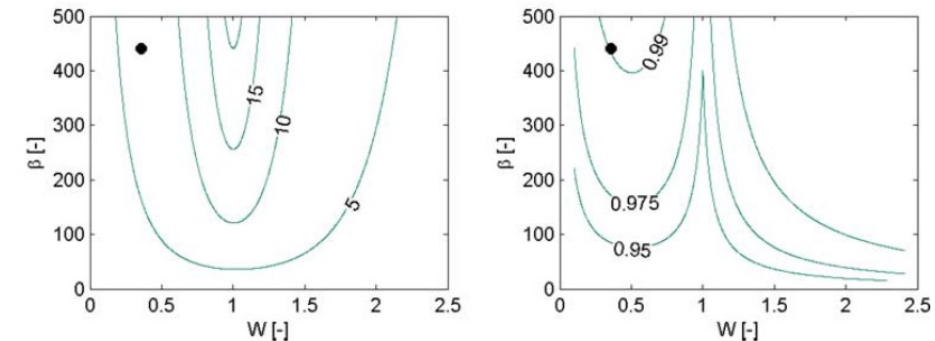
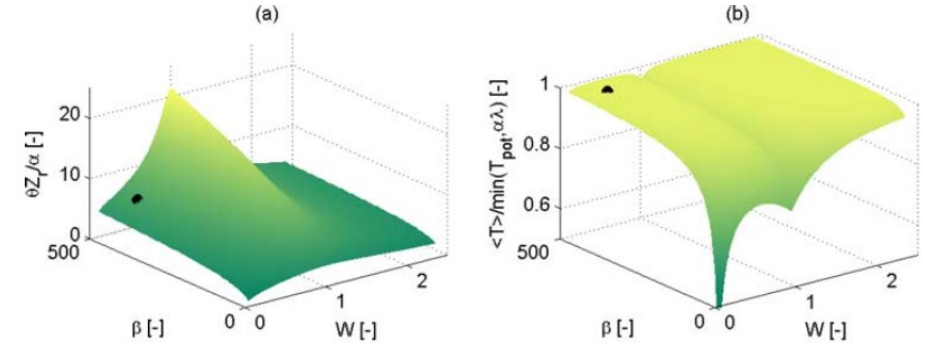
$$r(z) = \frac{\lambda_0 n (s_{fc} - \bar{s})}{T_p \bar{\rho}(s)} \{1 - P_H [nz(s_{fc} - \bar{s}_m(z))]\}$$



The American School, Optimization  
C cost & benefit (Guswa, WRR, 2008  
Guswa, WRR, 2010)

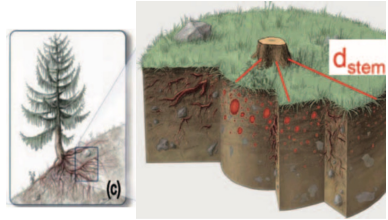
$$\frac{Z_r}{\alpha/\theta} = \frac{\ln \left( W \left[ 1 + \frac{1}{2} \beta (1 - W)^2 \pm \sqrt{\beta (1 - W)^2 + \left( \frac{1}{2} \beta (1 - W)^2 \right)^2} \right] \right)}{(1 - W)}$$

$$\beta = \frac{\theta}{\alpha A} = \frac{\theta}{\alpha} \cdot \frac{SRL \cdot WUE}{\gamma_r \cdot RLD} \cdot T_{pot} \cdot f_{seas}$$

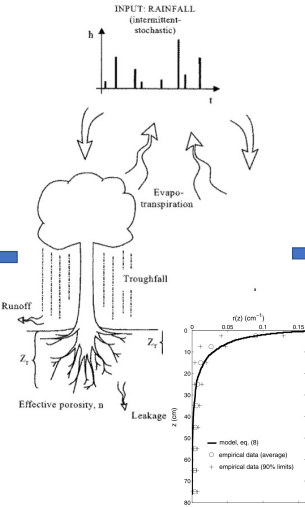


# Root Distribution Model (2D) Perona et al., Ecol. Eng. 2022

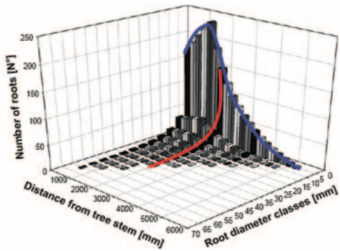
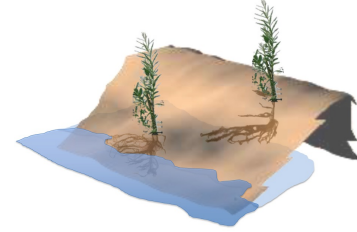
Schwarz et al. 2010



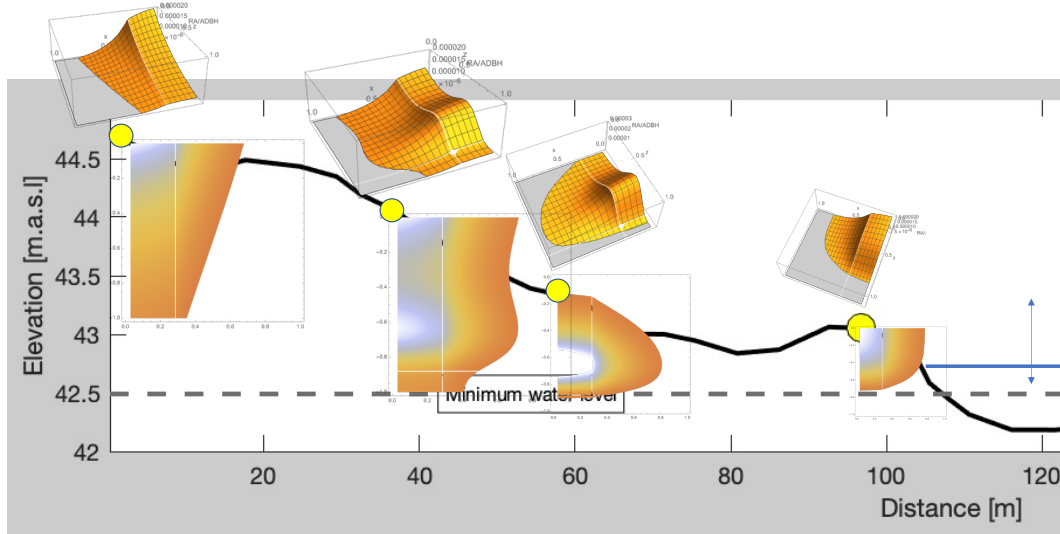
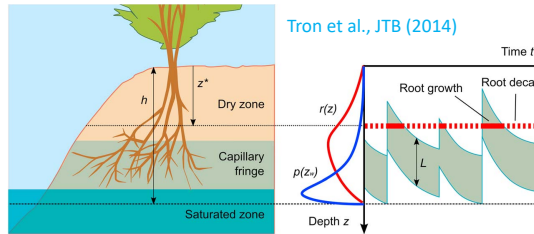
Laio et al. 2006



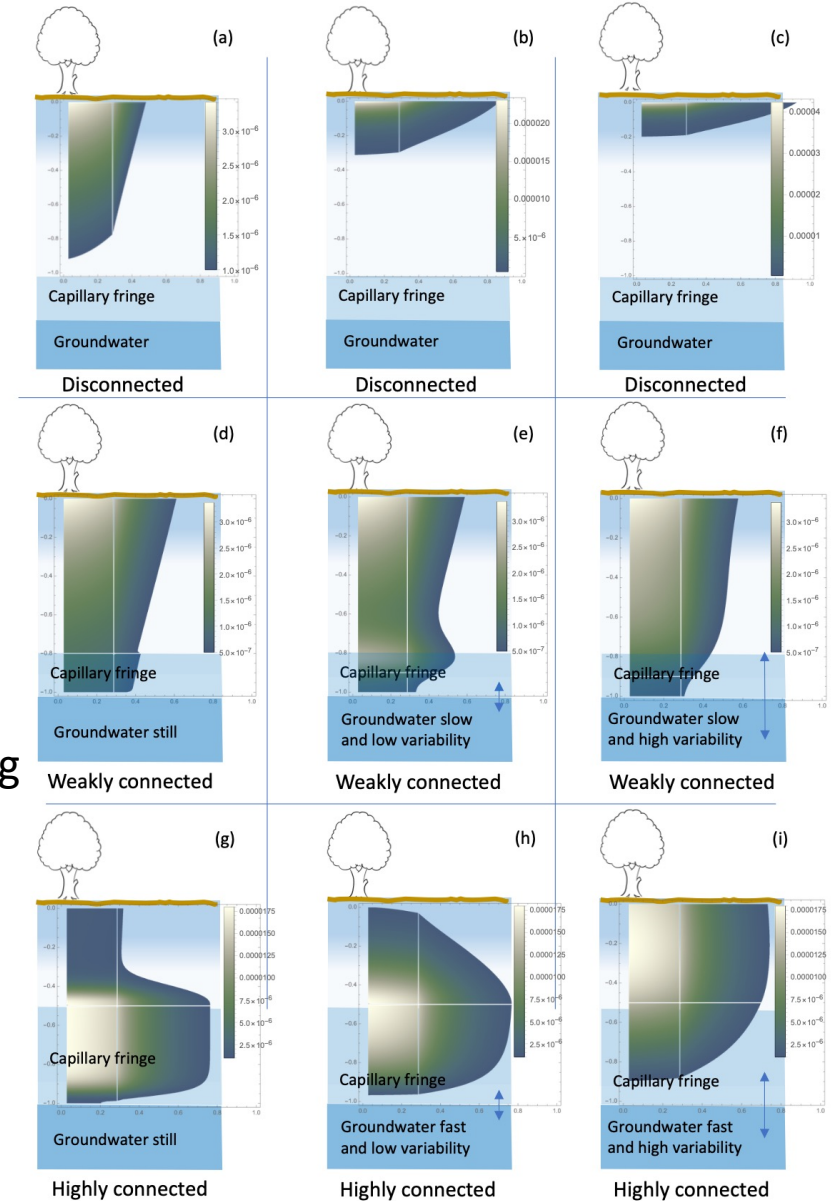
Tron et al. 2014



Tron et al., JTB (2014)

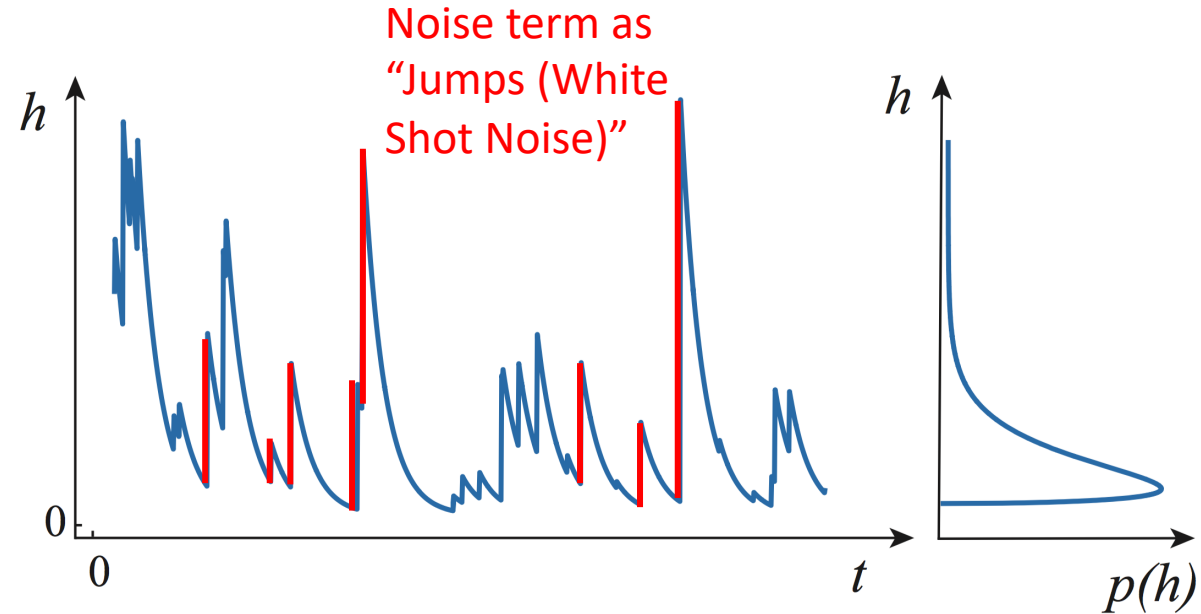
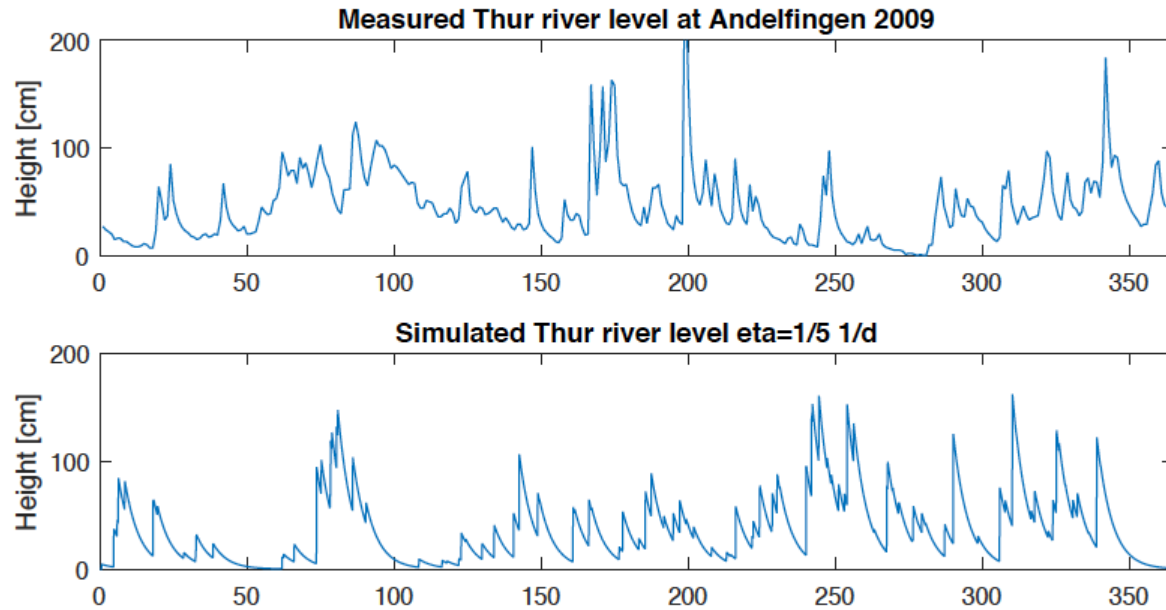


Awaiting for testing to crop plants under different tropism scenarios. Any interest?



# A stochastic model for riparian plant roots growth

(Tron et al., JTB 2014)



**FIRST: approximation of river fluctuations as a stochastic process driven by white shot noise:**

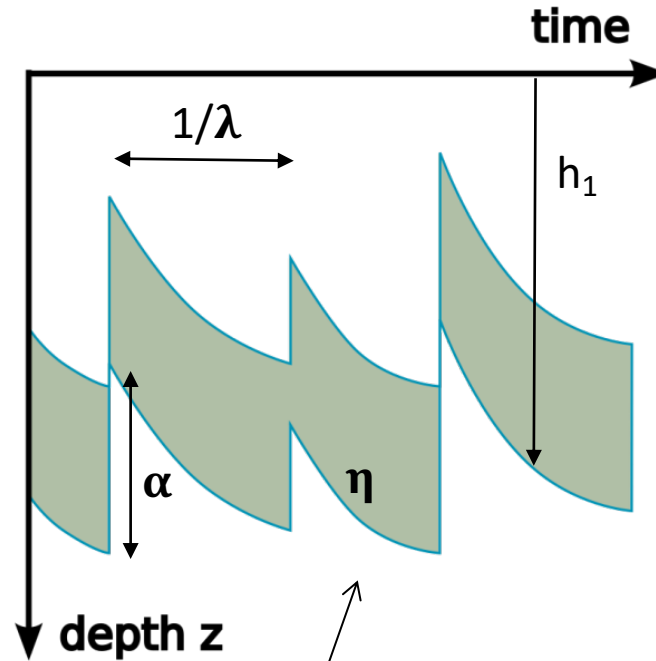
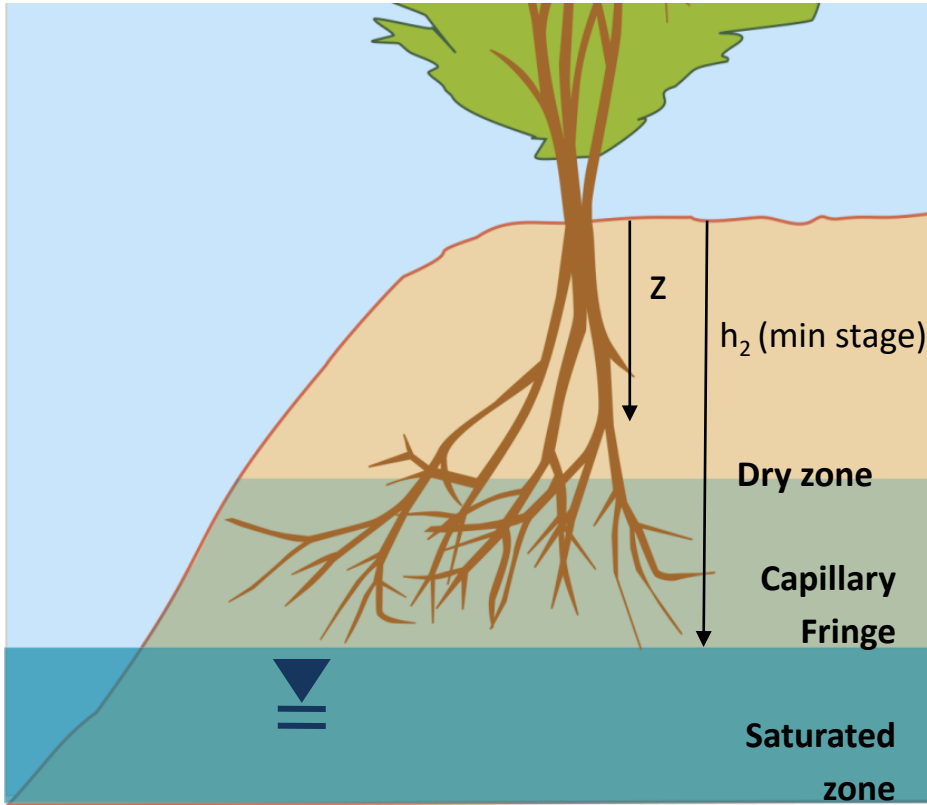
**Stochastic jumps (Poisson) + deterministic descends**

$$\frac{dh}{dt} = -\frac{h}{\tau} + \zeta(t)$$

**Compound Poisson Process**  
Cox and Miller (1969), Iturbe et al. (1999), Ridolfi et al. (2006), Botter et al. (2007)

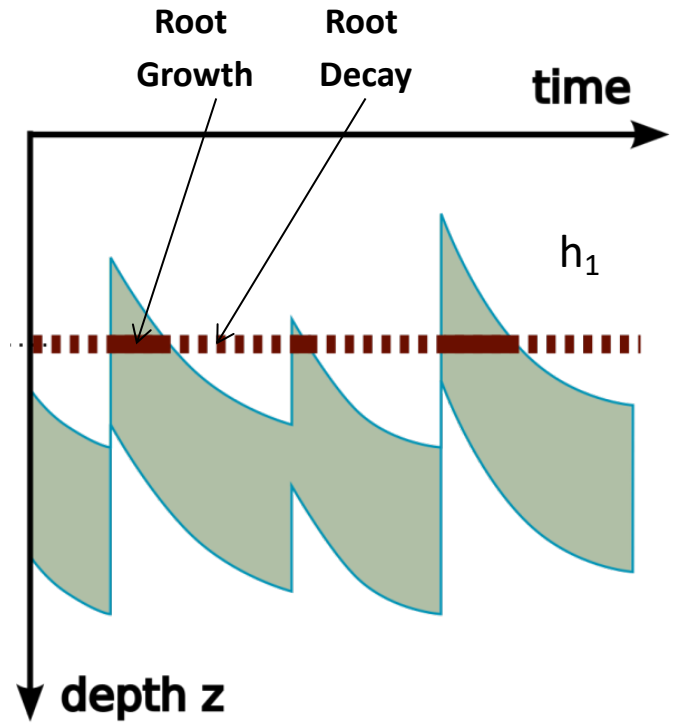
The pdf  $p(h)$  is analytical and is a Gamma function

The model is built considering that in riparian environments hydrotropism and aerotropism are the driving mechanisms controlling plant roots growth



Water table fluctuations

**DICHOTOMOUS NOISE**



Probability that a depth  $z$  is within the zone favourable for root growth

One obtains that the pdf of  $z_i = \tilde{z}_i / \tilde{h}_2$  is

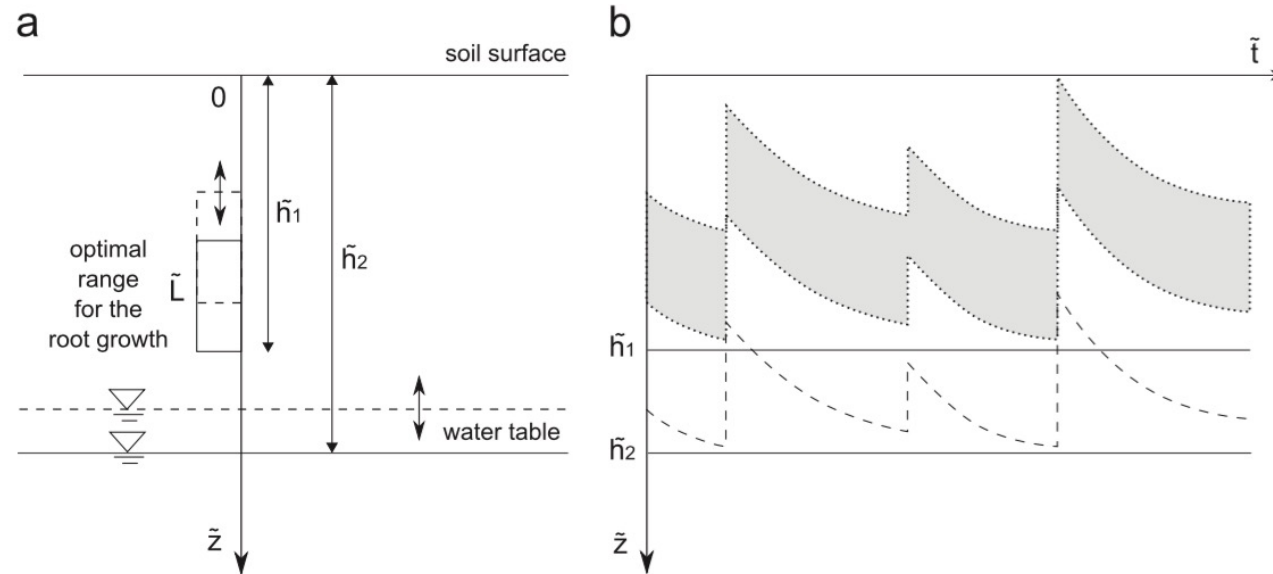
$$p(z_i) = \frac{\alpha^{-\lambda/\eta}}{\Gamma\left(\frac{\lambda}{\eta}\right)} e^{(z_i - h_1)/\alpha} (h_1 - z_i)^{\lambda/\eta - 1},$$

(Ridolfi et al., 2011)

**STOCHASTIC PROCESS DRIVEN BY WHITE SHOT NOISE**

$$k(z) = \begin{cases} \frac{\int_z^{\min[z+L, h_1]} p(z_i) dz_i}{\Gamma\left(\frac{\lambda}{\eta}\right)} & \text{if } -\infty < z < h_1 - L, \\ 1 - \frac{\Gamma\left(\frac{\lambda}{\eta}, \frac{h_1 - z}{\alpha}\right)}{\Gamma\left(\frac{\lambda}{\eta}\right)} & \text{if } h_1 - L < z < h_1, \end{cases}$$

# Dichotomous process for root growth and death



The telegraph process

$$\frac{dr(z)}{d\tilde{t}} = \begin{cases} \tilde{f}_1(r(z)) = \beta(z)(1-r(z)) & \text{if } z_i - L < z < z_i, \\ \tilde{f}_2(r(z)) = -\gamma r(z) & \text{if } z < z_i - L \vee z > z_i, \end{cases}$$



$$\frac{dr(z)}{dt} = \begin{cases} f_1(r(z)) = \theta(z)(1-r(z)) & \text{if } z_i - L < z < z_i, \\ f_2(r(z)) = -r(z) & \text{if } z < z_i - L \vee z > z_i, \end{cases}$$

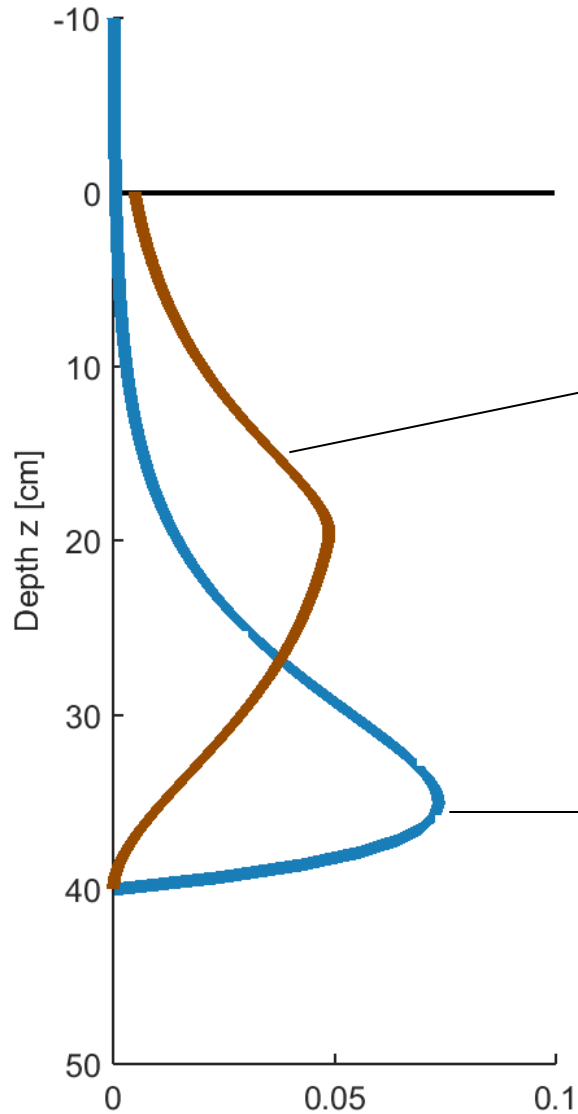
The dichotomous process is a stochastic process forced by the dichotomous noise  $\xi_{dn}$  which can assume only two values,  $\Delta_1$  and  $\Delta_2$ , with transition rate  $k_2$  for the transition  $\Delta_2 \rightarrow \Delta_1$ , and  $k_1$  for the transition  $\Delta_1 \rightarrow \Delta_2$ .

$$p(r(z)) = \frac{\Gamma\left(\frac{1}{\theta(z)} - \frac{k(z)}{\theta(z)} + k(z) + 1\right)}{\Gamma(k(z))\Gamma\left(\frac{1}{\theta(z)} - \frac{k(z)}{\theta(z)}\right)} (r(z) + \theta(z)(1-r(z))) \times (1-r(z))^{(1/\theta(z))(1-k(z))-1} r(z)^{k(z)-1},$$

Pdf of root density at a given depth,  $z$

Tron et al., 2014

This is the first model for root growth that has an analytical solution for the vertical profile (not a pdf!) of the biomass.



**ROOT PROFILE**  $r(z)$  is the mean of  $p(r(z))$  at given  $z$

$$\bar{r}(z) = \int_0^1 r(z) \cdot p(r(z)) dr = \frac{2\theta(z)k(z)}{\theta(z) + \theta(z)k(z) + 1 - k(z)}$$

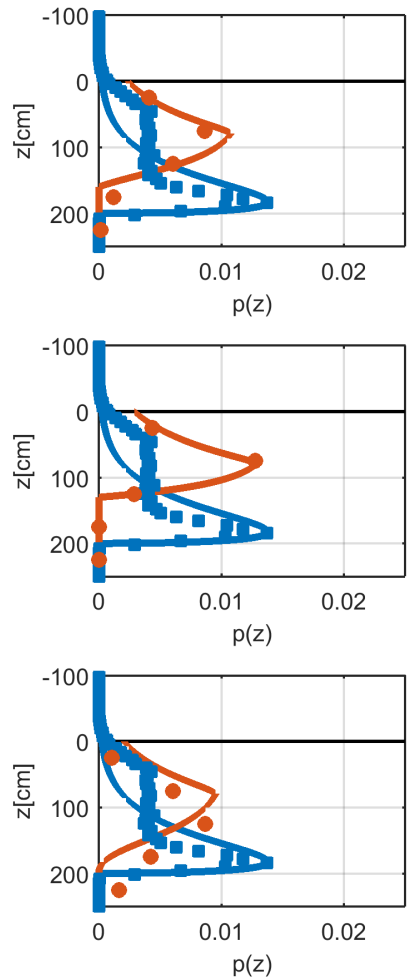
$$k(z) = \begin{cases} \left[ \Gamma\left(\tilde{\lambda}, \frac{h-z-L}{\alpha}\right) - \Gamma\left(\tilde{\lambda}, \frac{h-z}{\alpha}\right) \right] \cdot \Gamma(\tilde{\lambda})^{-1} & \text{if } -\infty < z < h - L, \\ 1 - \Gamma\left(\tilde{\lambda}, \frac{h-z}{\alpha}\right) \cdot \Gamma(\tilde{\lambda})^{-1} & \text{if } h - L < z < h, \end{cases}$$

**PDF of the WATER TABLE**  $p(z)$

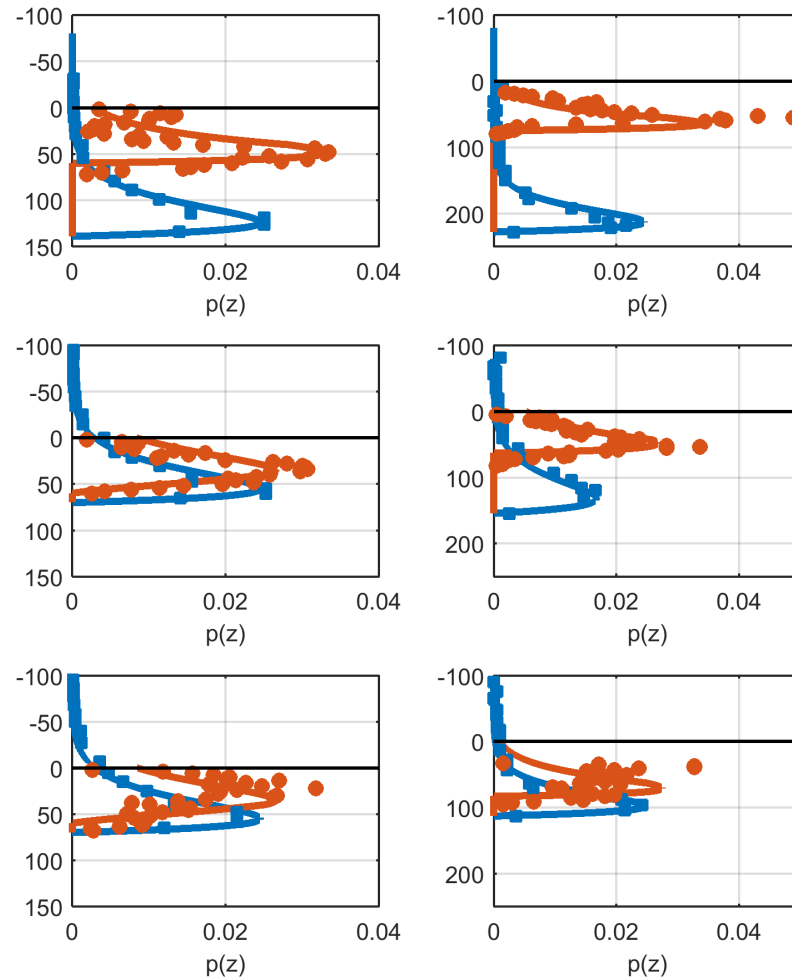
$$p(z) = \frac{-\tilde{\lambda}}{\Gamma(\tilde{\lambda})} e^{\frac{z-h}{\alpha}} (h-z)^{\tilde{\lambda}-1}$$

# Model validation

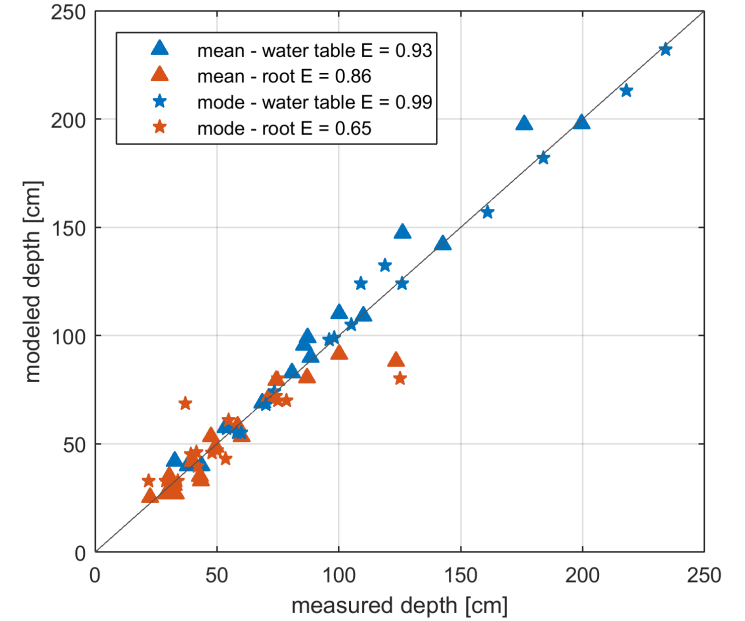
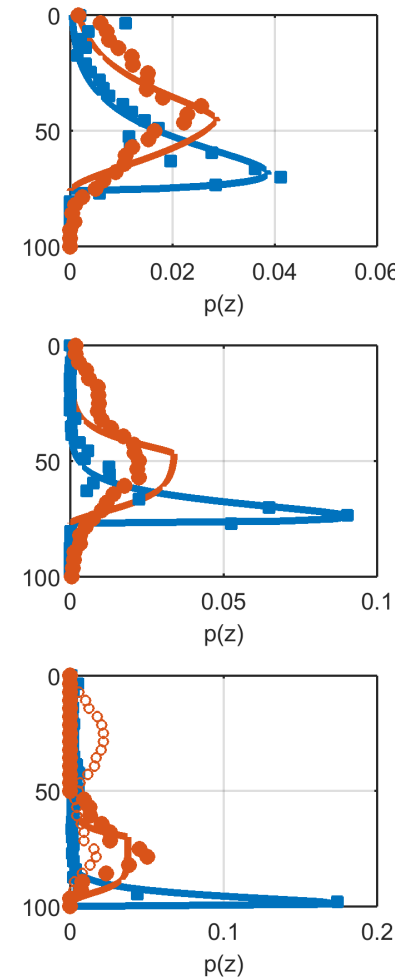
### 1. Rhone riverbank



### 2. Thur river island

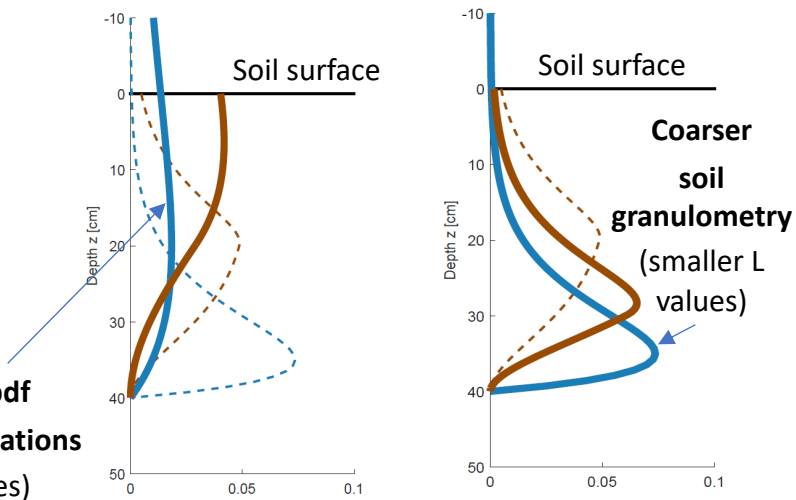
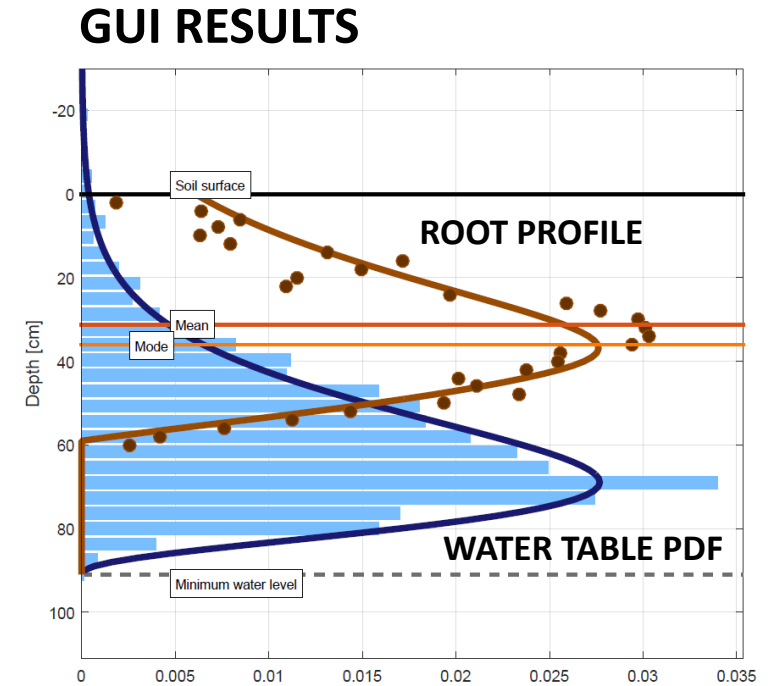
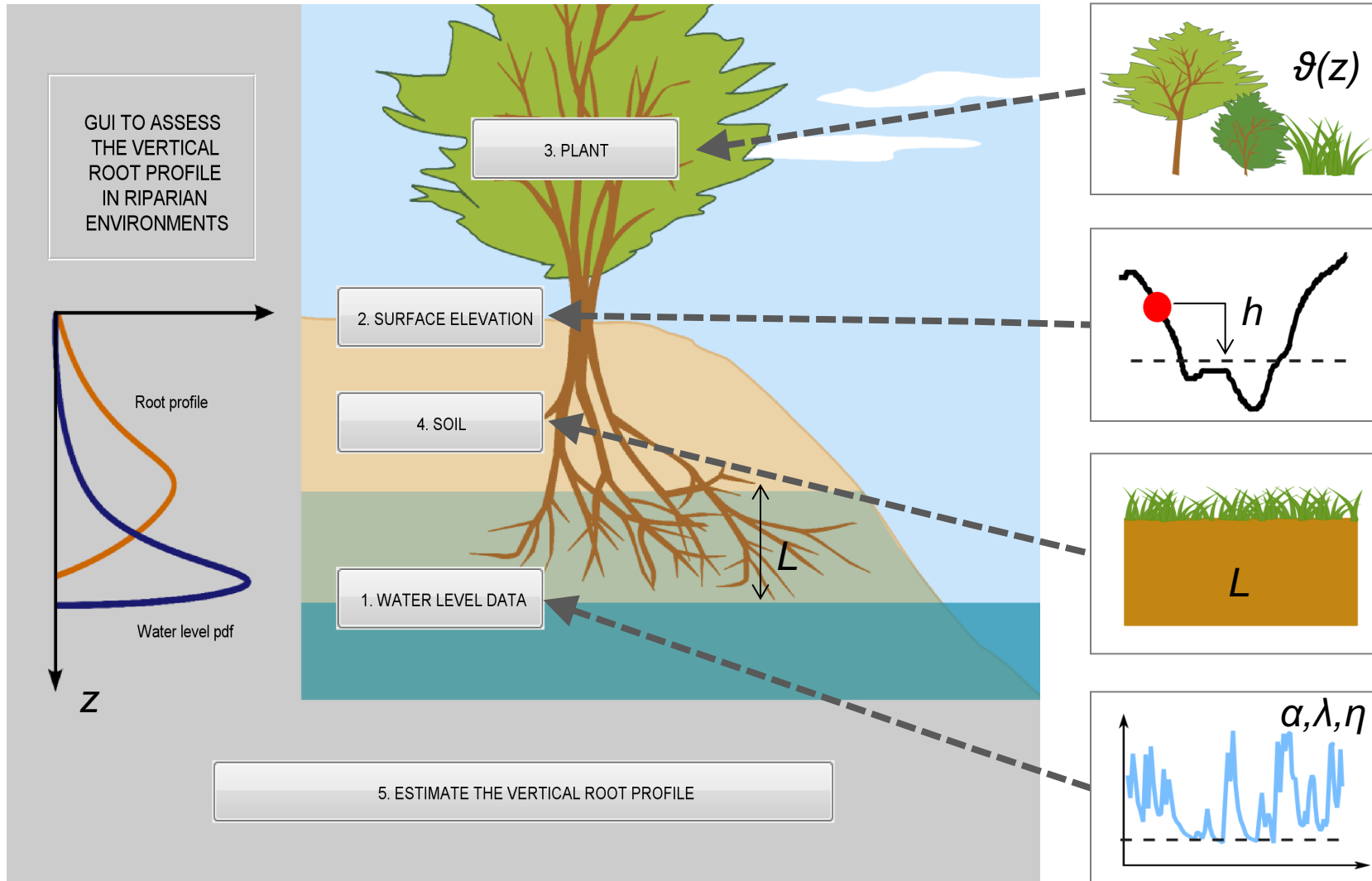


### 3. EPFL experiment

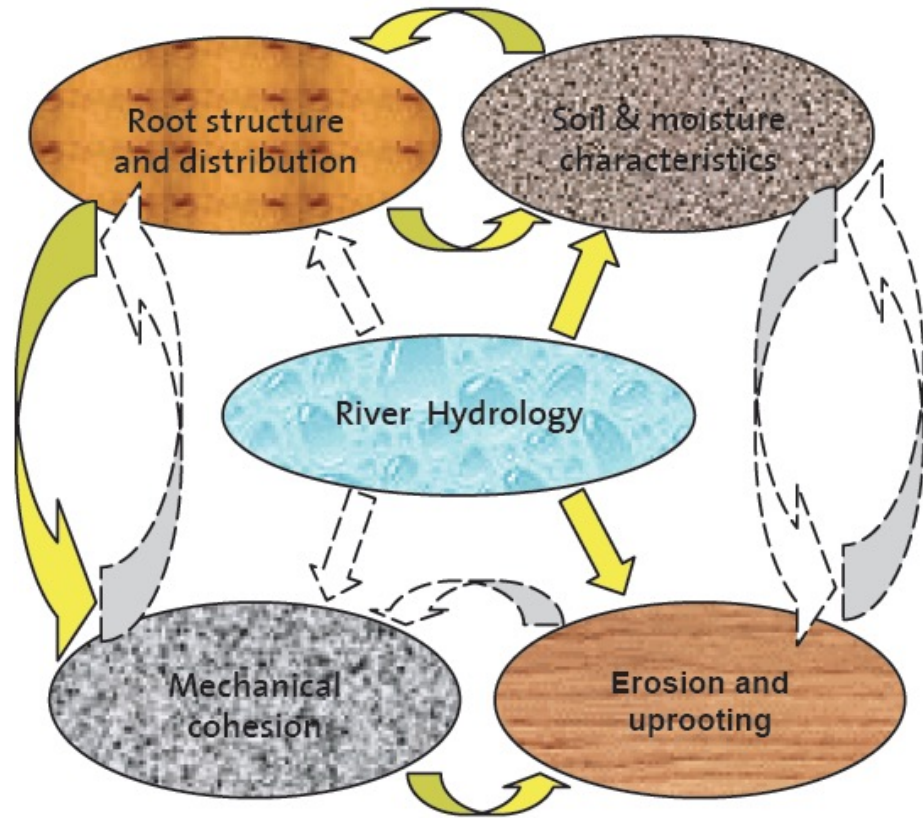


details in [Tron, Perona et al. \(2015\)](#)  
[Geophysical Research Letters](#)

# Root development graphical User Interface



# Some first conclusions



Growing roots at high elevations might be worth not only because floods come less frequently (hydrological return time): the deeper the roots are, the higher the actual return time of the flooding event that uproots the plant (continue...)

